

第十二章 回授與穩定度

- 回授的觀念
- 理想回授系統
- 四個理想回授電路之組態
 - 串-並(電壓)回授放大器
 - 並-串(電流)回授放大器
 - 串-串(轉移電導)回授放大器
 - 並-並(轉移電阻)回授放大器
- 回授電路之迴路增益
- 回授電路之穩定性準則
- 頻率補償技術
(藉由補償使得不穩定之回授電路能穩定)

第十二章 回授與穩定度

12.1 回授的觀念

兩種回授

正回授—輸入信號加上部份的輸出信號

負回授—輸入信號減掉部份的輸出信號

負回授的優點

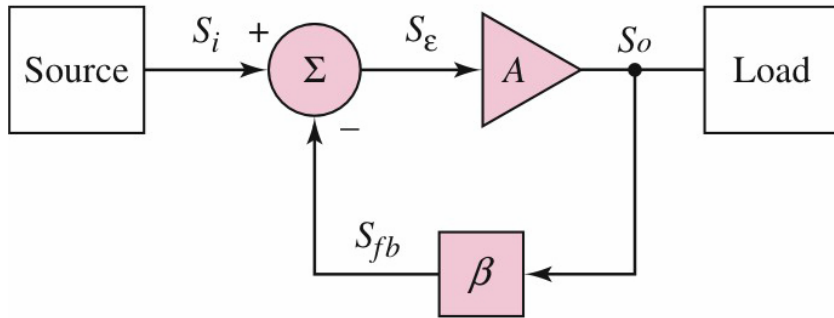
- 1) 減少增益的敏感度
- 2) 擴增電路的頻寬
- 3) 減少雜訊的敏感度
- 4) 減少非線性失真
- 5) 控制電路的輸入/出阻抗

負回授的缺點

- 1) 減少電路的增益
- 2) 減少電路的穩定性

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12.2 理想回授系統



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$$T = A\beta = \frac{S_{fb}}{S_\epsilon}$$

$$A\beta \gg 1 \rightarrow A_f \cong \frac{A}{A\beta} = \frac{1}{\beta}$$

非反相放大器(Non-inverting amplifier):

$$V_{fb} = \frac{R_1}{R_1 + R_2} V_o \rightarrow \beta = \frac{R_1}{R_1 + R_2}$$

$$\text{If } A\beta \gg 1, \quad A_f = \frac{V_o}{V_i} = \frac{1}{\beta} = 1 + \frac{R_2}{R_1}$$

$$S_o = AS_\epsilon; S_{fb} = \beta S_o; S_\epsilon = S_i - S_{fb}$$

$$S_o = A(S_i - \beta S_o) = AS_i - A\beta S_o$$

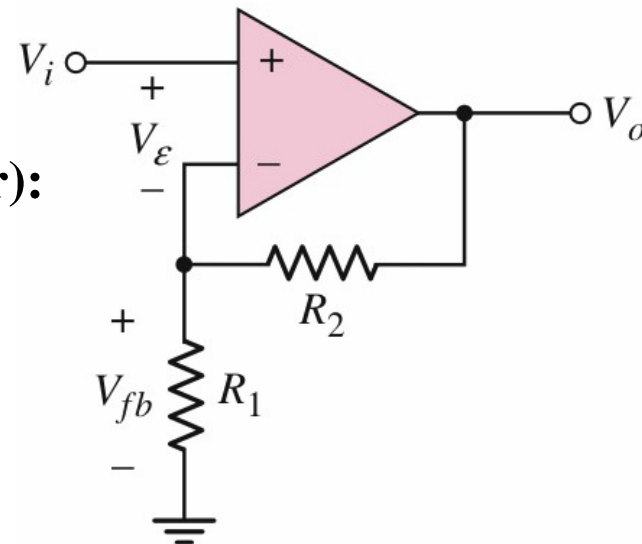
$$A_f = \frac{S_o}{S_i} = \frac{A}{1 + A\beta} = \frac{A}{1 + T}$$

A : 開迴路增益(open-loop gain)

β : 回授因子(feedback factor)

A_f : 閉迴路增益(closed-loop gain)

T = βA 為迴路增益(loop gain)



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增益的敏感度

$$\frac{dA_f}{dA} = \frac{1}{(1+\beta A)} - \frac{A}{(1+\beta A)^2} \cdot \beta = \frac{1}{(1+\beta A)^2}$$

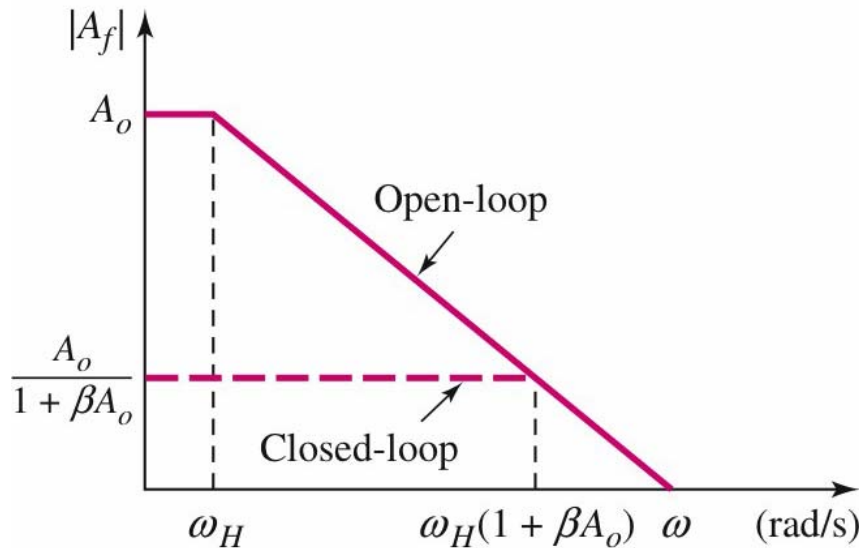
$$dA_f = \frac{dA}{(1+\beta A)^2}$$

$$\frac{dA_f}{A_f} = \frac{\frac{dA}{(1+\beta A)^2}}{\frac{A}{1+\beta A}} = \frac{1}{(1+\beta A)} \cdot \frac{dA}{A} = \left(\frac{A_f}{A} \right) \frac{dA}{A}$$

上式顯示出閉迴路增益 A_f 之改變量相較於開迴路增益之改變量約小 $(1+A\beta)$ 倍
→ 負回授減少增益的敏感度

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減少電路的增益與擴增電路的頻寬



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$$A(s) = \frac{A_0}{1 + \frac{s}{\omega_H}}$$

A_0 為低頻或中頻增益

ω_H 為上限3分貝轉角頻率

閉迴路增益為

$$A_f(s) = \frac{A}{1 + \beta A} = \frac{A_0}{(1 + \beta A_0)} \cdot \frac{1}{1 + \frac{s}{\omega_H(1 + \beta A_0)}}$$

低頻閉迴路增益

$$\frac{A_0}{(1 + \beta A_0)}$$

閉迴路頻寬乘積為

$$\omega_H(1 + \beta A_0)$$

低頻閉迴路增益與閉迴路頻寬的乘積為

$$\frac{A_0}{(1 + \beta A_0)} [\omega_H(1 + \beta A_0)] = A_0 \omega_H$$

第十二章 回授與穩定度

降低雜訊的敏感度

負回授可降低放大器的雜訊準位(更精確來說負回授可增加信號對雜訊比值)

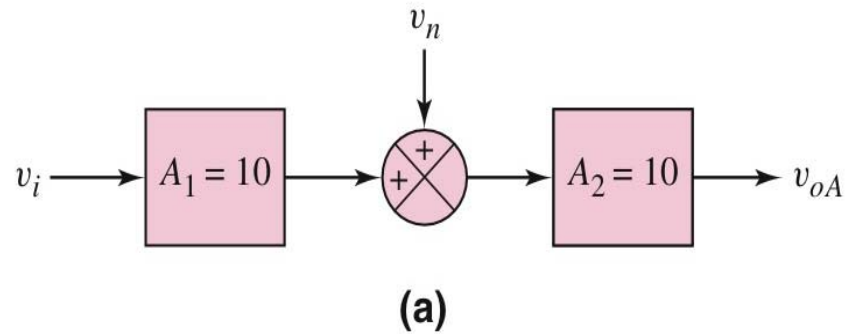
輸入之信號對雜訊比值為

$$(\text{SNR})_i = \frac{S_i}{N_i} = \frac{v_i}{v_n}$$

輸出之信號對雜訊比值為

$$(\text{SNR})_o = \frac{S_o}{N_o} = \frac{A_{Ti} S_i}{A_{Tn} N_i}$$

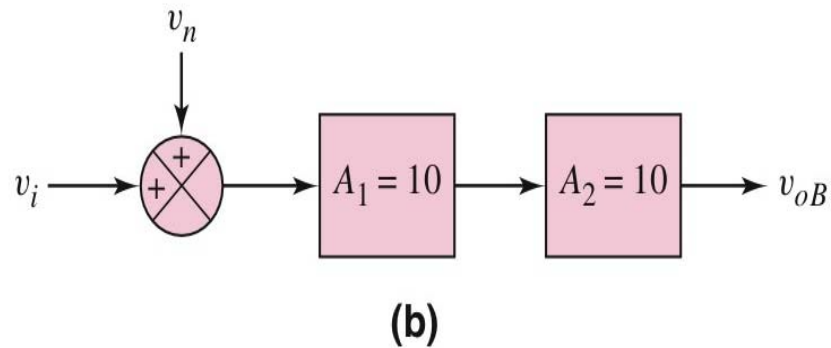
第十二章 回授與穩定度



由圖 (a)

$$v_{oA} = A_1 A_2 v_i + A_2 v_n = 100v_i + 10v_n$$

$$\frac{S_o}{N_o} = \frac{100v_i}{10v_n} = 10 \frac{S_i}{N_i}$$

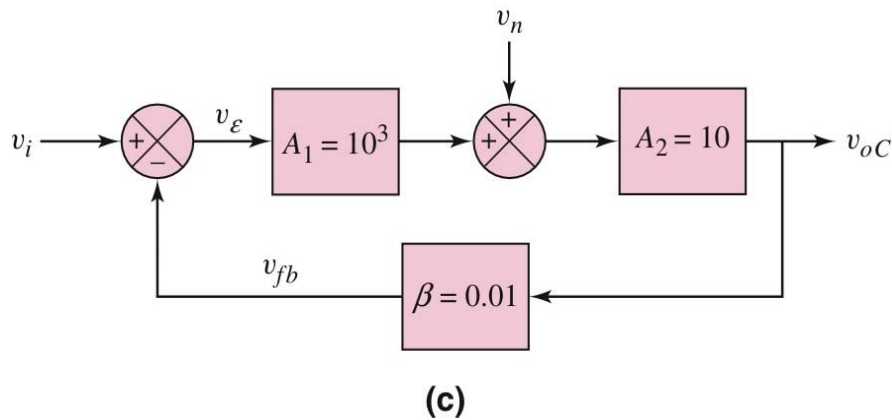


由圖 (b)

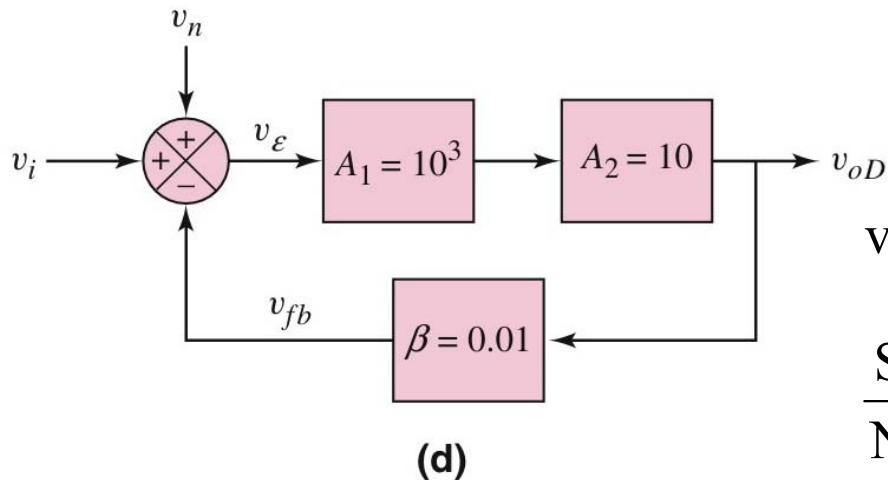
$$v_{oB} = A_1 A_2 v_i + A_1 A_2 v_n = 100v_i + 100v_n$$

$$\frac{S_o}{N_o} = \frac{100v_i}{100v_n} = \frac{S_i}{N_i}$$

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由圖 (c)

$$v_{oc} = A_1 A_2 v_{\epsilon} + A_2 v_n$$

$$v_{fb} = \beta v_{oc} \quad v_{\epsilon} = v_i - v_{fb} = v_i - \beta v_{oc}$$

$$v_{oc} = A_1 A_2 (v_i - \beta v_{oc}) + A_2 v_n$$

$$= \frac{A_1 A_2}{(1 + \beta A_1 A_2)} \cdot v_i + \frac{A_2}{(1 + \beta A_1 A_2)} \cdot v_n$$

$$\cong 100v_i + 0.1v_n$$

$$\frac{S_0}{N_0} = \frac{100v_i}{0.1v_n} = 1000 \frac{S_i}{N_i}$$

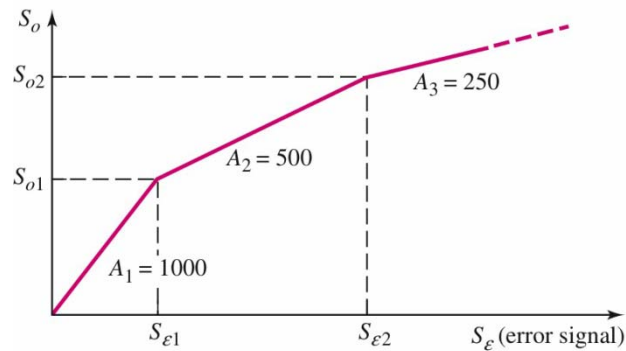
由圖 (d)

$$v_{od} = \frac{A_1 A_2}{(1 + \beta A_1 A_2)} \cdot (v_i + v_n) \cong 100v_i + 100v_n$$

$$\frac{S_0}{N_0} = \frac{100v_i}{100v_n} = \frac{S_i}{N_i}$$

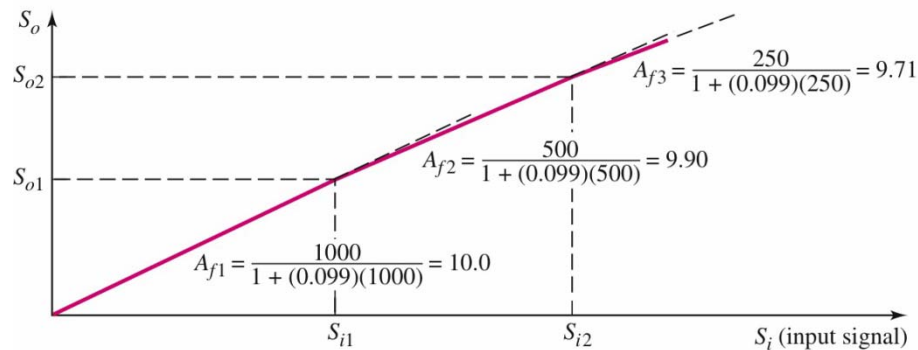
第十二章 回授與穩定度

減少非線性失真



(a)

圖 (a) 為基本放大器(開迴路)轉換特性。式子中顯現增益隨輸入信號改變而改變。



(b)

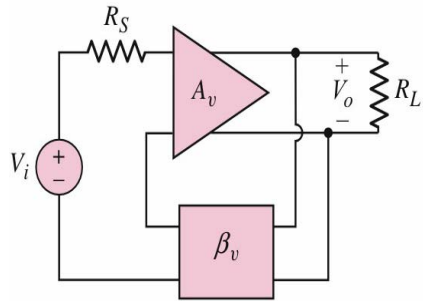
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圖 (b) 閉迴路轉換特性

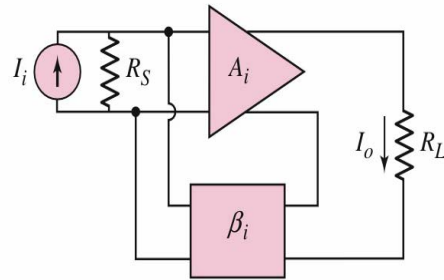
開迴路增益變動 2 倍時，其閉迴路增益只改變 1% 及 2%。

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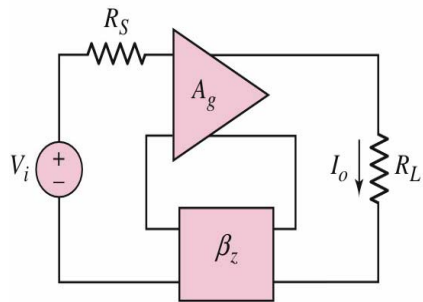
12.3 四個理想回授電路之組態



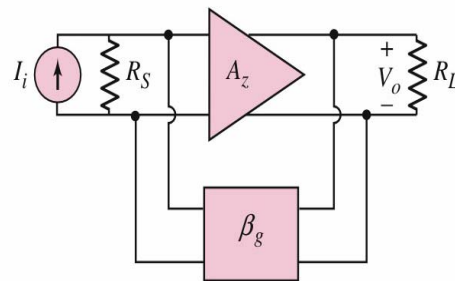
(a) Series-shunt



(b) Shunt-series



(c) Series-series



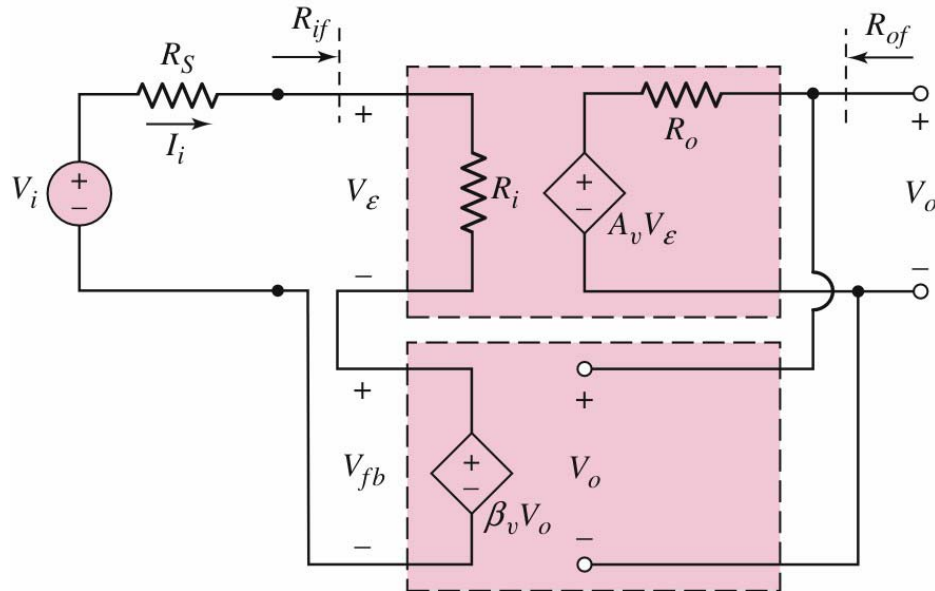
(d) Shunt-shunt

依照放大參數(電壓或電流)與輸出參數(電壓或電流)的不同，回授技術可分為四類：

- (a) 串-並 \Rightarrow 電壓放大器
- (b) 並-串 \Rightarrow 電流放大器
- (c) 串-串 \Rightarrow 轉導放大器
- (d) 並-並 \Rightarrow 轉阻放大器

第十二章 回授與穩定度

● 串-並組態(電壓放大器)



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$$V_o = A_v V_\varepsilon$$

$$V_{fb} = \beta V_o = \beta_v V_o$$

$$V_\varepsilon = V_i - V_{fb}$$

$$A_{vf} = \frac{V_o}{V_i} = \frac{A_v}{(1 + \beta_v A_v)} \quad \text{閉迴路電壓增益}$$

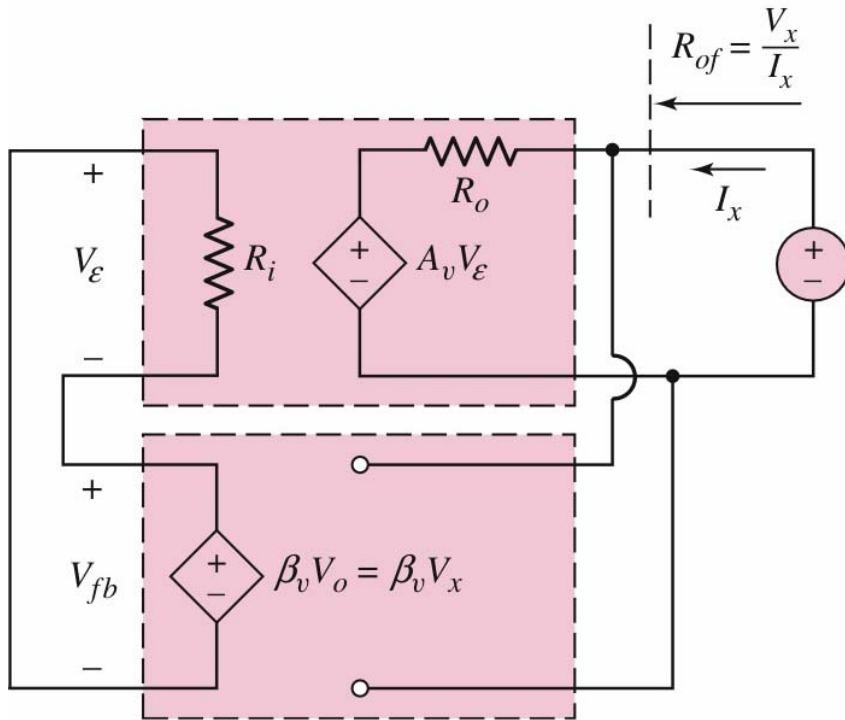
$$\begin{aligned} V_i &= V_\varepsilon + V_{fb} = V_\varepsilon + \beta_v V_o \\ &= V_\varepsilon + \beta_v (A_v V_\varepsilon) \end{aligned}$$

$$V_\varepsilon = \frac{V_i}{(1 + \beta_v A_v)}$$

$$I_i = \frac{V_\varepsilon}{R_i} = \frac{V_i}{R_i (1 + \beta_v A_v)}$$

$$R_{if} = \frac{V_i}{I_i} = R_i (1 + \beta_v A_v) \quad \text{輸入電阻} \uparrow$$

第十二章 回授與穩定度



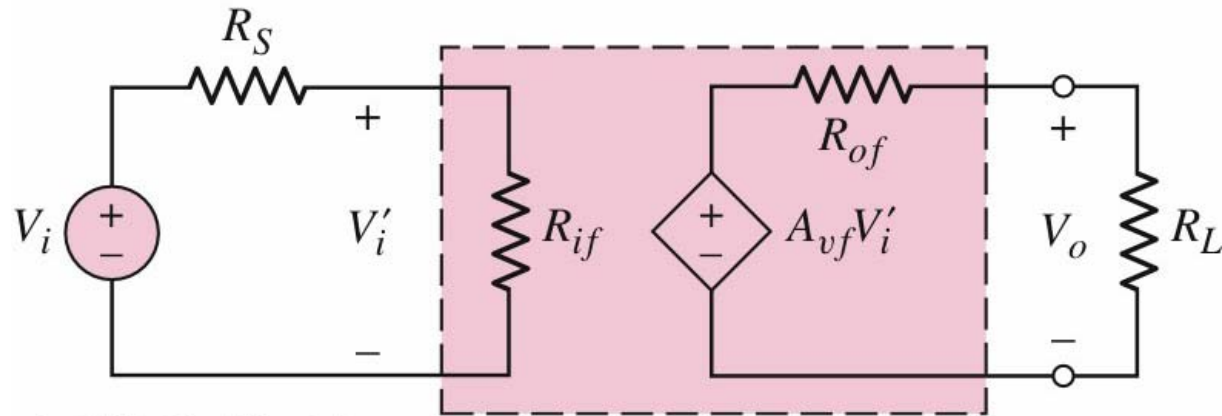
$$V_\epsilon + V_{fb} = V_\epsilon + \beta_v V_x = 0$$

$$V_\epsilon = -V_{fb} = -\beta_v V_x$$

$$I_x = \frac{V_x - A_v V_\epsilon}{R_o} = \frac{V_x - A_v (-\beta_v V_x)}{R_o} = \frac{V_x (1 + \beta_v A_v)}{R_o}$$

$$R_{of} = \frac{V_x}{I_x} = \frac{R_o}{(1 + \beta_v A_v)} \quad \text{輸出電阻} \downarrow$$

第十二章 回授與穩定度



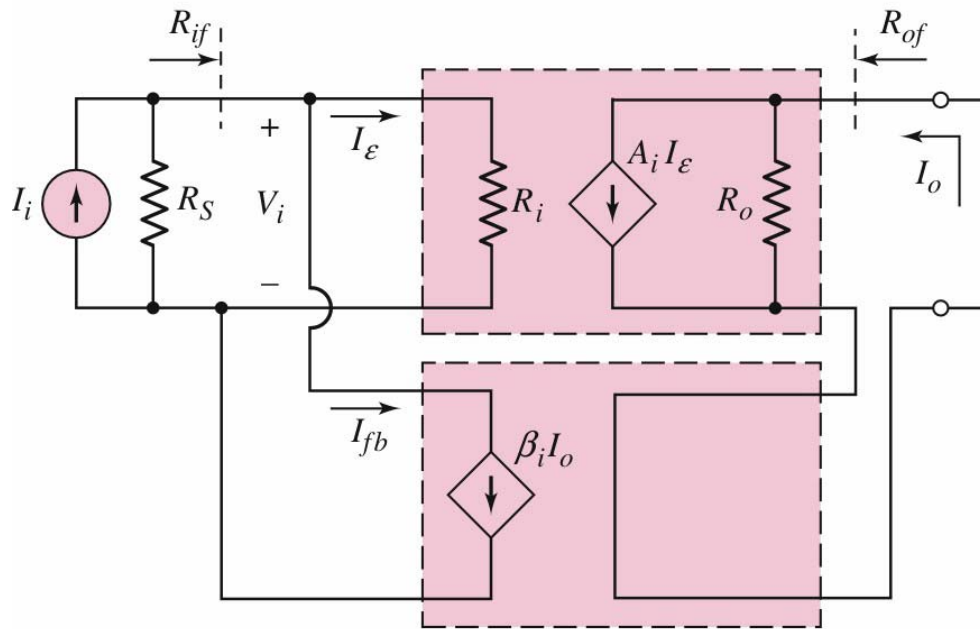
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串-並回授電路或電壓放大器之等效電路

$$A_{vf} = \frac{A_v}{(1 + \beta_v A_v)}; \quad R_{of} = \frac{R_0}{(1 + \beta_v A_v)}; \quad R_{if} = R_i(1 + \beta_v A_v)$$

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● 並-串組態(電流放大器)



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$$I_o = A_i I_\varepsilon$$

$$I_{fb} = \beta I_o = \beta_i I_o$$

$$I_i = I_\varepsilon + I_{fb}$$

$$A_{if} = \frac{I_o}{I_i} = \frac{A_i}{(1 + \beta_i A_i)} \quad \text{閉迴路電流增益}$$

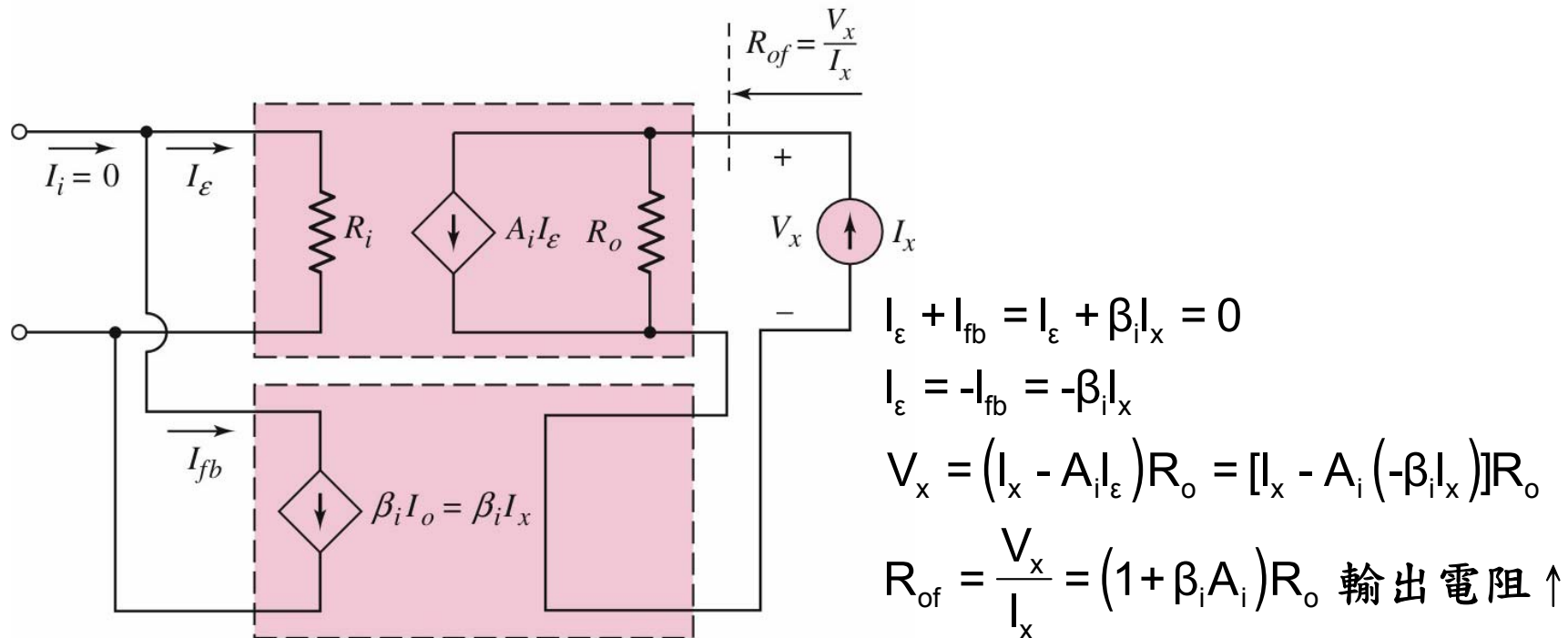
$$I_i = I_\varepsilon + I_{fb} = I_\varepsilon + \beta_i I_o = I_\varepsilon + \beta_i (A_i I_\varepsilon)$$

$$I_\varepsilon = \frac{I_i}{(1 + \beta_i A_i)}$$

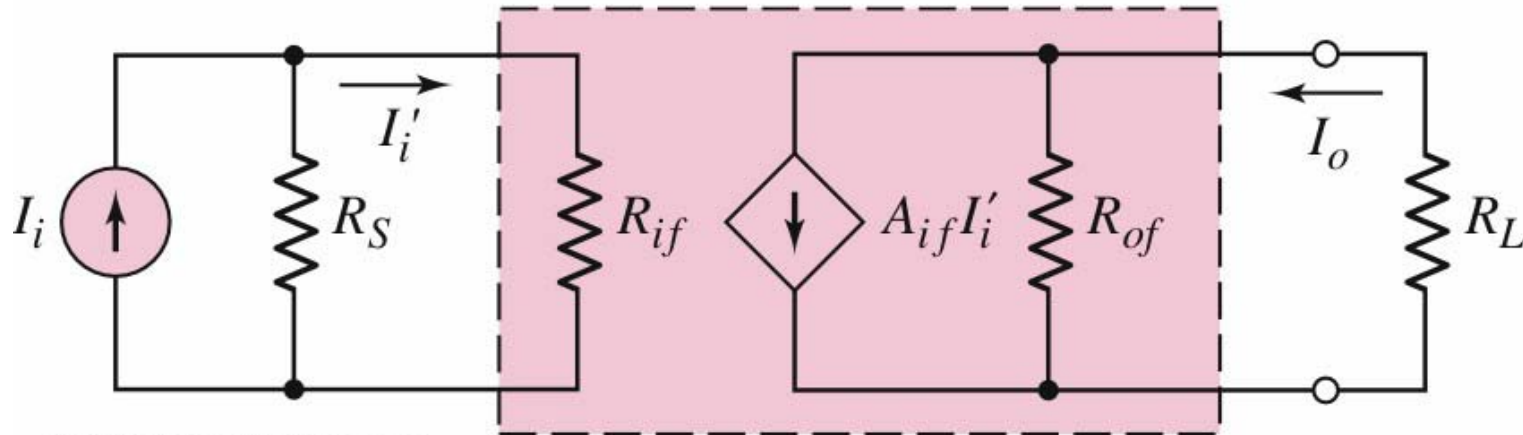
$$V_i = I_\varepsilon R_i = \frac{I_i R_i}{(1 + \beta_i A_i)}$$

$$R_{if} = \frac{V_i}{I_i} = \frac{R_i}{(1 + \beta_i A_i)} \quad \text{輸入電阻} \downarrow$$

第十二章 回授與穩定度



第十二章 回授與穩定度



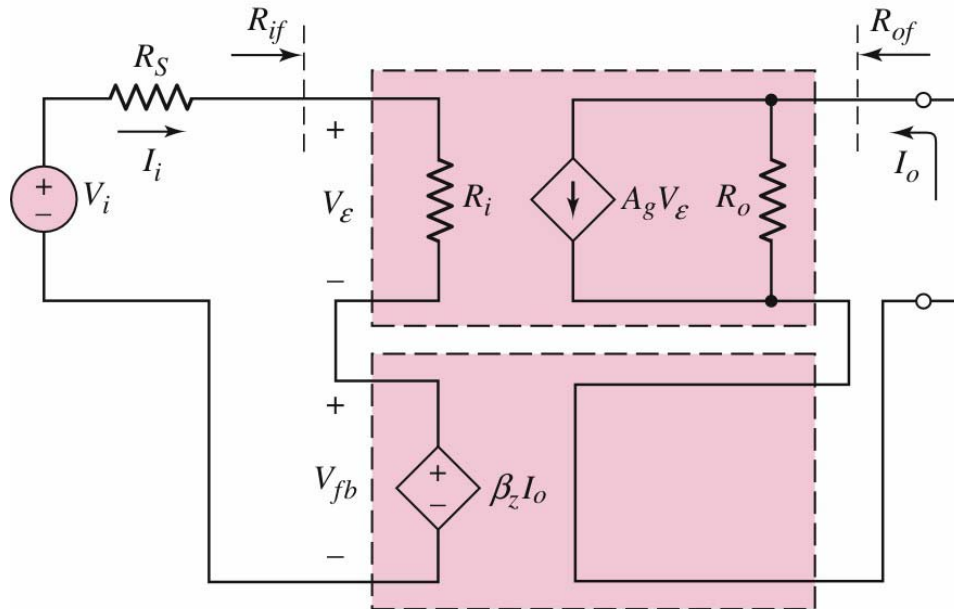
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並-串回授電路或電流放大器之等效電路

$$A_{if} = \frac{A_i}{(1 + \beta_i A_i)}; \quad R_{if} = \frac{R_i}{(1 + \beta_i A_i)}; \quad R_{of} = R_o (1 + \beta_i A_i)$$

第十二章 回授與穩定度

● 串-串組態(轉導放大器)



$$I_o = A_g V_\epsilon$$

$$V_{fb} = \beta_z I_o$$

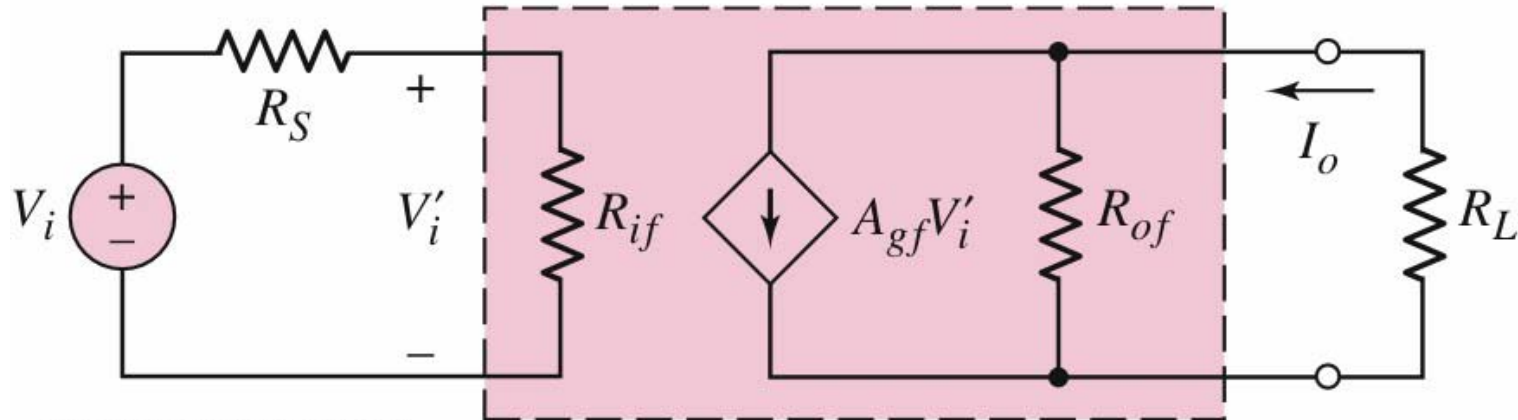
$$V_i = V_\epsilon + V_{fb}$$

$$A_{gf} = \frac{I_o}{V_i} = \frac{A_g}{(1 + \beta_z A_g)}$$

$$R_{if} = \frac{V_i}{I_i} = R_i (1 + \beta_z A_g) \quad \text{輸入電阻} \uparrow$$

$$R_{of} = \frac{V_o}{I_o} = R_o (1 + \beta_z A_g) \quad \text{輸出電阻} \uparrow$$

第十二章 回授與穩定度



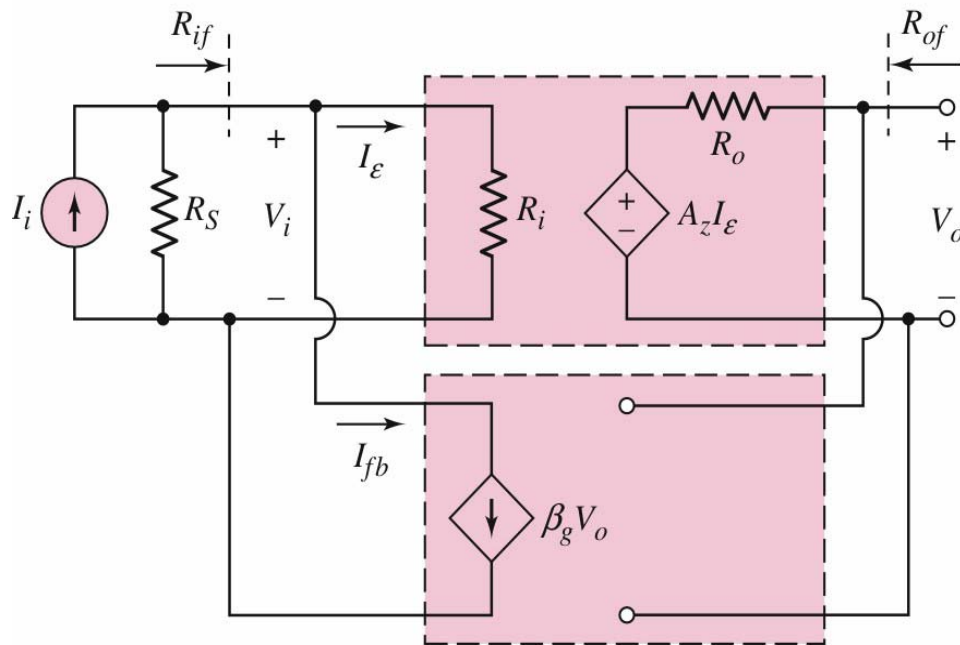
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串-串回授電路或轉導放大器之等效電路

$$A_{gf} = \frac{A_g}{(1 + \beta_z A_g)}; \quad R_{if} = R_i (1 + \beta_z A_g); \quad R_{of} = R_o (1 + \beta_z A_g)$$

第十二章 回授與穩定度

● 並-並組態 (轉阻放大器)



$$V_o = A_z I_\epsilon$$

$$I_{fb} = \beta_g V_o$$

$$I_i = I_\epsilon + I_{fb}$$

$$A_{zf} = \frac{V_o}{I_i} = \frac{A_z}{(1 + \beta_g A_z)}$$

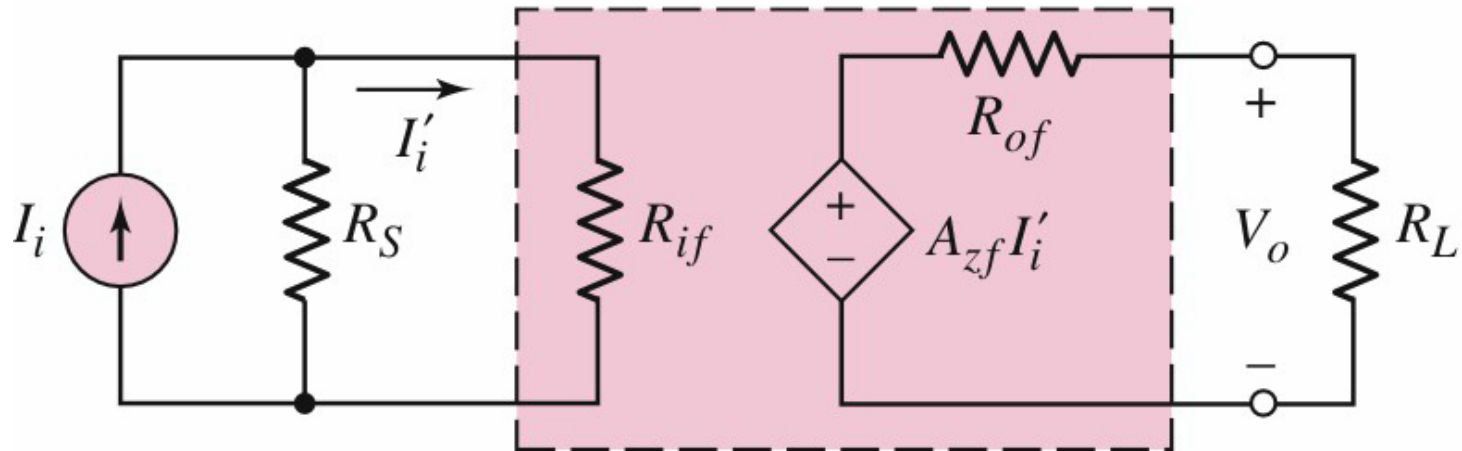
$$R_{if} = \frac{V_i}{I_i} = \frac{R_i}{(1 + \beta_g A_z)}$$

$$R_{of} = \frac{V_o}{I_o} = \frac{R_o}{(1 + \beta_g A_z)}$$

輸入電阻 ↓

輸出電阻 ↓

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並-並回授電路或轉導放大器之等效電路

$$A_{zf} = \frac{A_z}{(1 + \beta_g A_z)}; \quad R_{if} = \frac{R_i}{(1 + \beta_g A_z)}; \quad R_{of} = \frac{R_o}{(1 + \beta_g A_z)}$$

12.21 Consider the noninverting op-amp circuit in Figure P12.20. The input resistance of the op-amp is $R_i = \infty$ and the output resistance is $R_o = 0$, but the op-amp has a finite gain A .

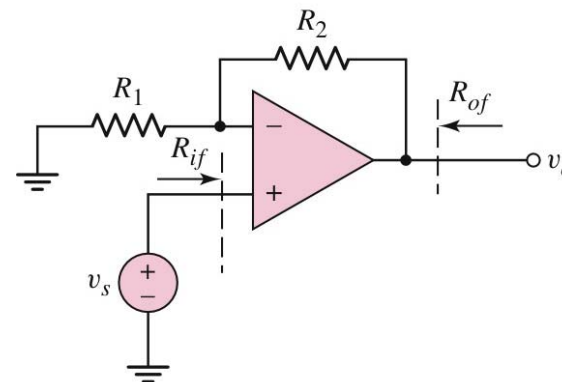
(a) Write the closed-loop transfer function in the form

$$A_{vf} = \frac{v_o}{v_s} = \frac{A}{(1 + \beta A)}$$

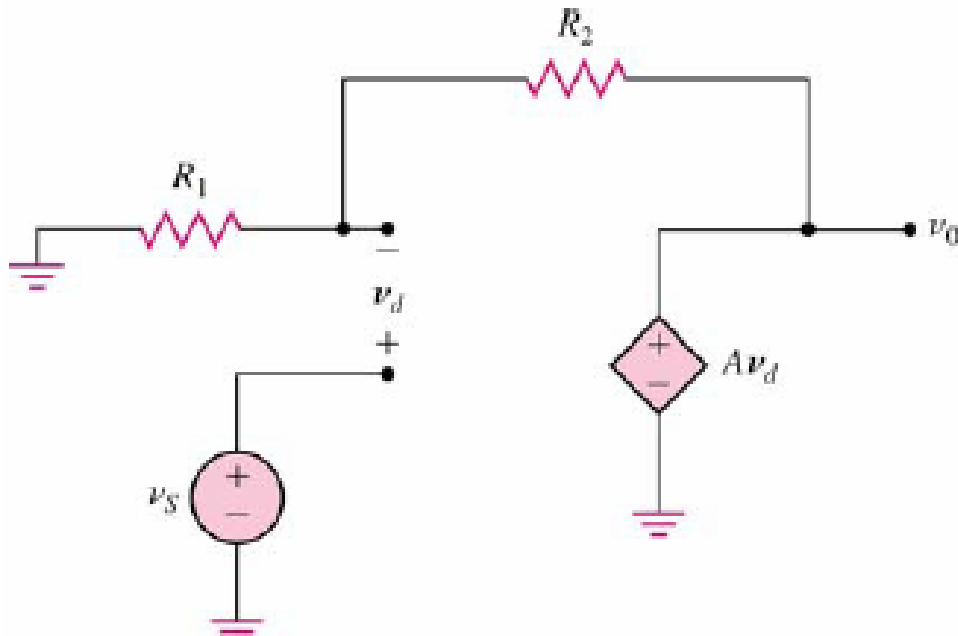
(b) What is the expression for β ?

(c) If $A = 10^5$ and $A_{vf} = 20$, what is the required β and R_2/R_1 ?

(d) If A decreases by 10%, what is the % change in A_{vf} ?



a.



$$\frac{v_s - v_d}{R_1} = \frac{v_0 - (v_s - v_d)}{R_2} \text{ and } v_d = \frac{v_0}{A}$$

$$v_s \left(\frac{1}{R_1} + \frac{1}{R_2} \right) = \frac{v_0}{R_2} \left[1 + \frac{1}{A} \left(1 + \frac{R_2}{R_1} \right) \right]$$

$$A_f = \frac{v_0}{v_s} = \frac{A}{1 + \left[A / \left(1 + \frac{R_2}{R_1} \right) \right]}$$

b.

$$\beta = \frac{1}{1 + \frac{R_2}{R_1}}$$

c.

$$20 = \frac{10^5}{1 + (10^5)\beta}$$

$$\text{So } \beta = \frac{\frac{10^5}{20} - 1}{10^5} \Rightarrow \underline{\beta = 0.04999}$$

$$\text{Then } \frac{R_2}{R_1} = \frac{1}{\beta} - 1 = \frac{1}{0.04999} - 1$$

$$\Rightarrow \underline{\frac{R_2}{R_1} = 19.004}$$

d.

$$A \rightarrow 9 \times 10^4$$

$$A_f = \frac{9 \times 10^4}{1 + (9 \times 10^4)(0.04999)} = 19.99956$$

$$\frac{\Delta A_f}{A_f} = \frac{-4.444 \times 10^{-4}}{20} = -2.222 \times 10^{-3}\%$$

$$\Rightarrow \underline{\frac{\Delta A_f}{A_f} = -0.005\%}$$

12.24 Consider the op-amp circuit in Figure P12.24.

The op-amp has a finite gain, so that $i_o = A_i i_\epsilon$, and a zero output impedance.

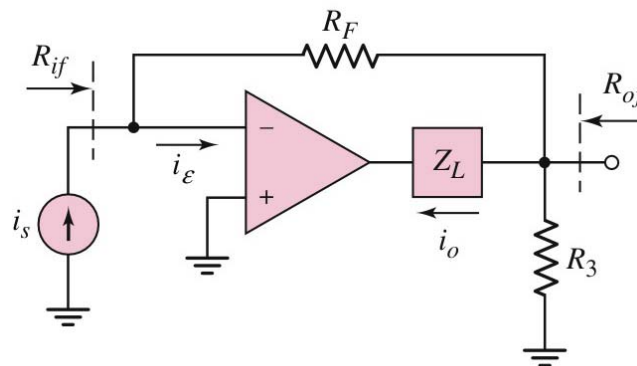
(a) Write the closed-loop transfer function in the form

$$A_{if} = \frac{i_o}{i_s} = \frac{A_i}{(1 + \beta_i A_i)}$$

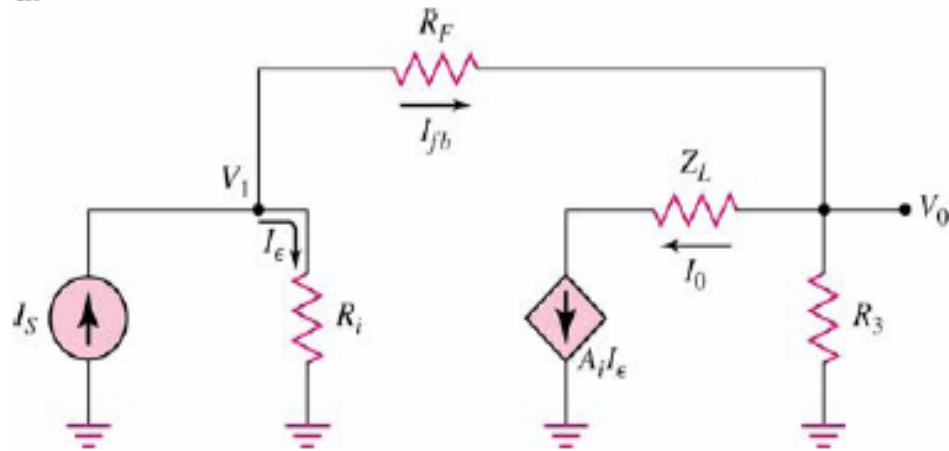
(b) What is the expression for β_i ?

(c) If $A_i = 10^5$ and $A_{if} = 25$, what is the required β_i and R_F/R_3 ?

(d) If A_i decreases by 15%, what is the % change in A_{if} ?



a.



Assume that V_1 is at virtual ground. $V_0 = -I_{j_b} R_F$

$$I_{j_b} = I_0 + \frac{V_0}{R_3} = I_0 - \frac{I_{j_b} R_F}{R_3}$$

$$I_{j_b} = I_S - I_e \quad \text{and} \quad I_0 = A_i I_e = \frac{I_0}{A_i}$$

$$\text{so } I_{j_b} = I_S - \frac{I_0}{A_i}$$

$$I_0 = I_{j_b} \left(1 + \frac{R_F}{R_3} \right) = \left(I_S - \frac{I_0}{A_i} \right) \left(1 + \frac{R_F}{R_3} \right)$$

$$A_v = \frac{I_0}{I_S} = \frac{\left(1 + \frac{R_F}{R_3} \right)}{\left[1 + \frac{1}{A_i} \left(1 + \frac{R_F}{R_3} \right) \right]} = \frac{A_i}{1 + \frac{A_i}{\left(1 + \frac{R_F}{R_3} \right)}} = A_v$$

b.
$$\beta_i = \frac{1}{\left(1 + \frac{R_F}{R_3} \right)}$$

c.
$$25 = \frac{10^5}{1 + (10^5)\beta_i}$$

$$\text{so } \beta_i = \frac{10^5 - 1}{25 \cdot 10^5} \Rightarrow \underline{\beta_i = 0.03999}$$

$$\text{so } \frac{R_F}{R_3} = \frac{1}{\beta_i} - 1 = \frac{1}{0.03999} - 1 \Rightarrow \underline{\frac{R_F}{R_3} = 24.0}$$

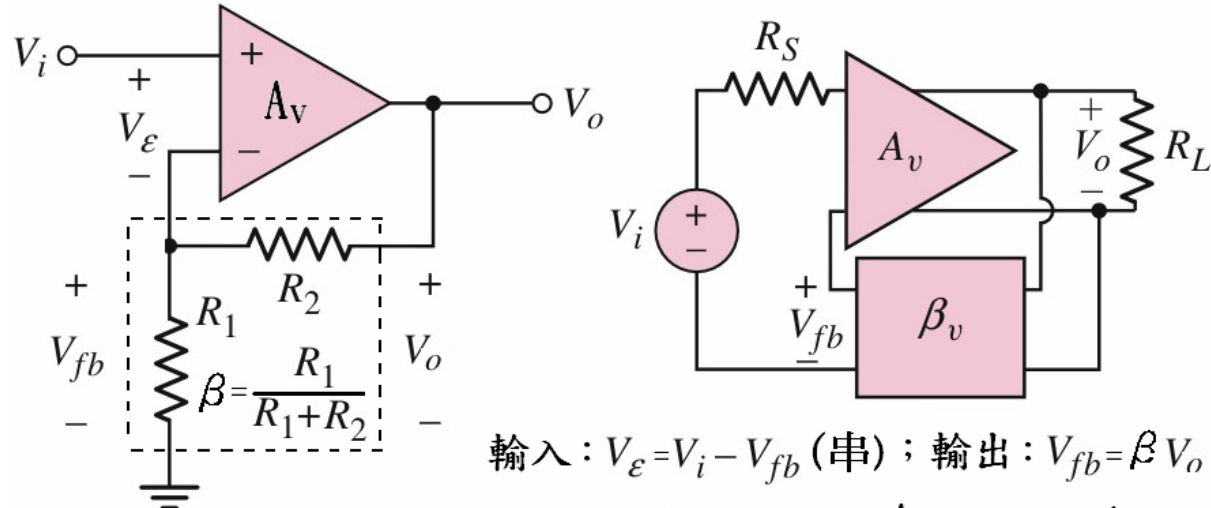
d.
$$A_i = 10^5 - (0.15)(10^5) = 8.5 \times 10^4$$

$$\text{so } A_v = \frac{8.5 \times 10^4}{1 + (8.5 \times 10^4)(0.03999)} = 24.9989$$

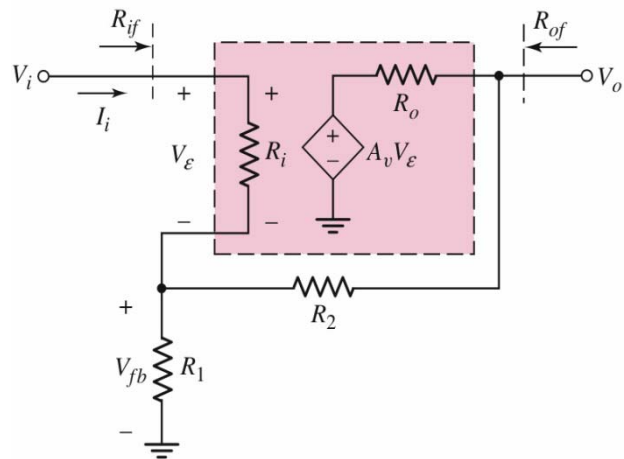
$$\text{so } \frac{\Delta A_v}{A_v} = -\frac{1.10 \times 10^{-3}}{25} = -4.41 \times 10^{-5} \Rightarrow \underline{-4.41 \times 10^{-3} \%}$$

第十二章 回授與穩定度

12.4 串-並回授組態



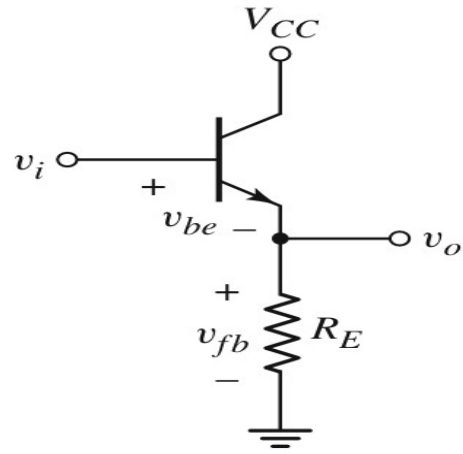
$$V_o = A_v V_{\epsilon} = A_v (V_i - V_{fb}) = A_v (V_i - \beta V_o) \rightarrow A_{vf} = \frac{V_o}{V_i} = \frac{A_v}{1 + A_v \beta} = \frac{A_v}{1 + A_v \frac{R_1}{R_1 + R_2}}$$



$$V_i = V_s + \left(\frac{R_1}{R_1 + R_2} \right) V_o = V_s + \frac{A_v V_s}{\left(1 + \frac{R_2}{R_1} \right)} = V_s \left[1 + \frac{A_v}{\left(1 + \frac{R_2}{R_1} \right)} \right]$$

$$R_{if} = \frac{V_i}{I_i} = \frac{V_i}{(V_s / R_1)} = R_1 \left[1 + \frac{A_v}{\left(1 + \frac{R_2}{R_1} \right)} \right] = R_1 (1 + \beta_v A_v)$$

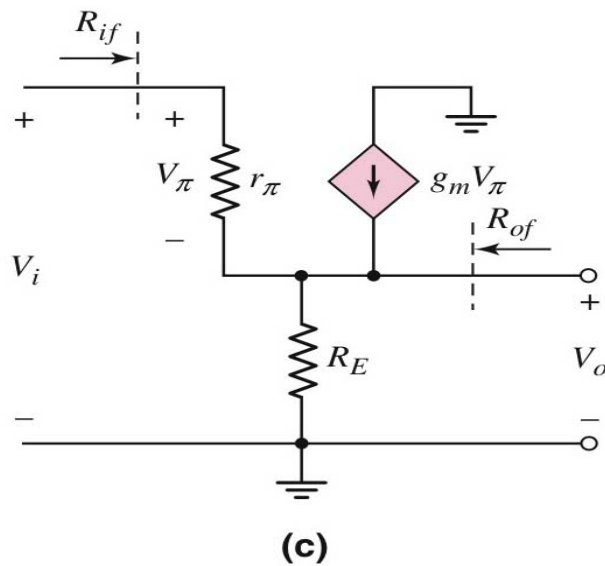
第十二章 回授與穩定度



$$A_{vf} = \frac{V_o}{V_i} = \frac{\left(\frac{1}{r_\pi} + g_m\right) R_E}{1 + \left(\frac{1}{r_\pi} + g_m\right) R_E} = \frac{\frac{R_E}{r_e}}{1 + \frac{R_E}{r_e}}$$

$$r_e = \frac{r_\pi}{1 + g_m r_\pi}$$

$$A_v = \left(\frac{1}{r_\pi} + g_m\right) R_E = \frac{R_E}{r_e} ; \beta = 1, (V_o = V_{fb})$$



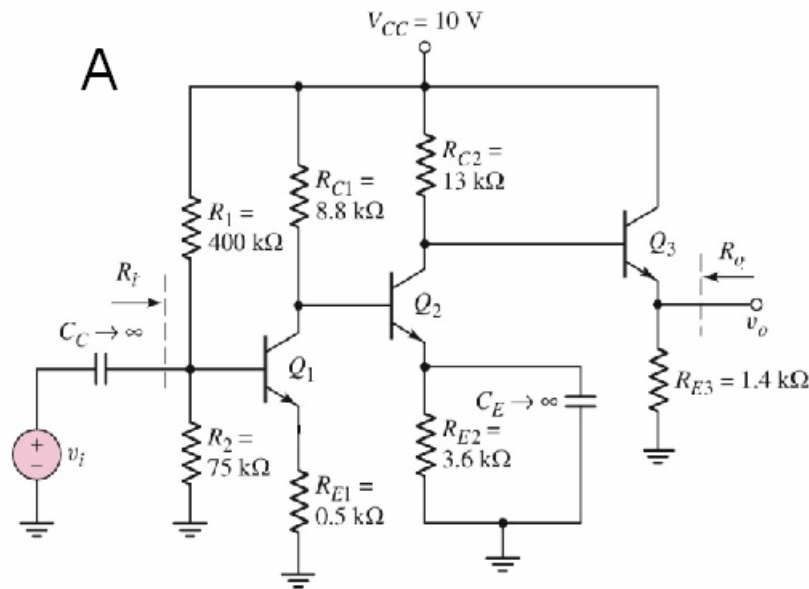
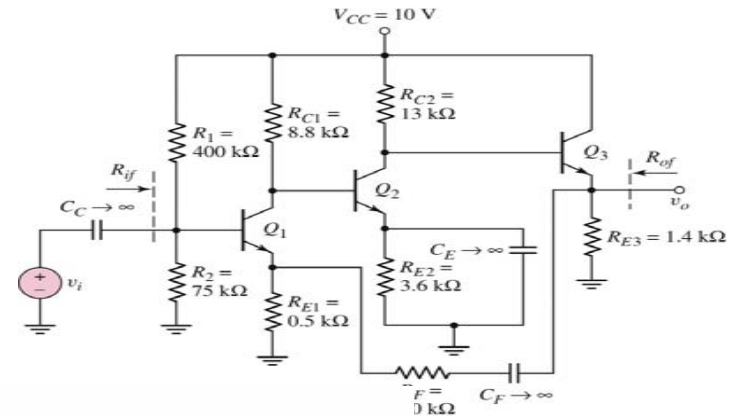
$$R_{if} = r_\pi + (1 + h_{FE}) R_E = r_\pi \left[1 + \left(\frac{1}{r_\pi} + g_m\right) R_E \right]$$

$$R_{of} = R_E \parallel \frac{r_\pi}{(1 + h_{FE})} = R_E \parallel r_e$$

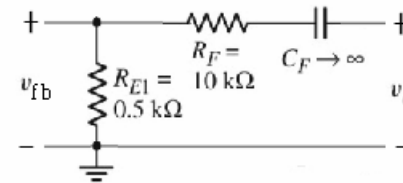
$$R_{of} = \frac{R_E}{1 + \left(\frac{1}{r_\pi} + g_m\right) R_E}$$

Draw the circuits of basic blocks A and β , and find the value of β .

Ans:

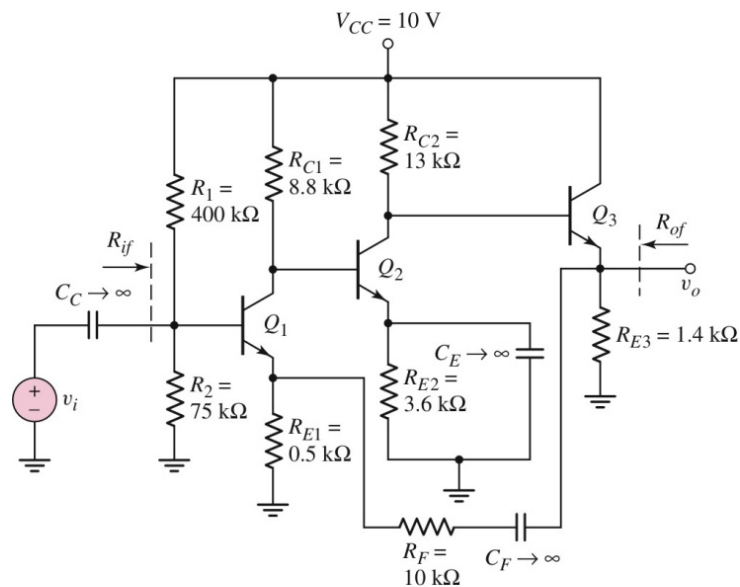


β



$$\beta = \frac{R_{E1}}{R_F + R_{E1}} = \frac{0.5K}{10K + 0.5K} = 1/21$$

12.36 Consider the series-shunt feedback circuit in Figure P12.36, with transistor parameters: $h_{FE}=120$, $V_{BE(on)}=0.7V$, and $V_A=\infty$. (a) Determine the small-signal parameters for Q_1 , Q_2 , and Q_3 . Using nodal analysis, determine: (b) the small-signal voltage gain $A_{vf}=v_o/v_i$. (c) the input resistance R_{if} , and (d) the output resistance R_{of} .



a. $R_{TH} = R_1 \parallel R_2 = 400 \parallel 75 = 63.2 \text{ k}\Omega$

$$V_{TH} = \left(\frac{R_2}{R_1 + R_2} \right) V_{CC} = \left(\frac{75}{75 + 400} \right) (10) = 1.579 \text{ V}$$

$$I_{BQ1} = \frac{1.579 - 0.7}{63.2 + (121)(0.5)} = 0.007106 \text{ mA}$$

$$I_{CQ1} = 0.853 \text{ mA}$$

$$V_{C1} = 10 - (0.853)(8.8) = 2.49 \text{ V}$$

$$I_{C2} \approx \frac{2.49 - 0.7}{3.6} = 0.497 \text{ mA}$$

$$V_{C2} = 10 - (0.497)(13) = 3.54 \text{ V}$$

$$I_{C3} \approx \frac{3.54 - 0.7}{1.4} = 2.03 \text{ mA}$$

Then

$$r_{\pi 1} = \frac{(120)(0.026)}{0.853} = 3.66 \text{ k}\Omega$$

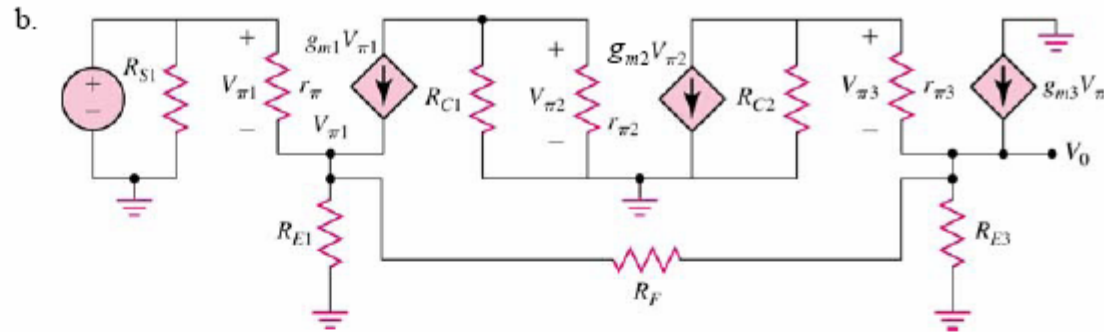
$$g_{m1} = \frac{0.853}{0.026} = 32.81 \text{ mA/V}$$

$$r_{\pi 2} = \frac{(120)(0.026)}{0.497} = 6.28 \text{ k}\Omega$$

$$g_{m2} = \frac{0.497}{0.026} = 19.12 \text{ mA/V}$$

$$r_{\pi 3} = \frac{(120)(0.026)}{2.03} = 1.54 \text{ k}\Omega$$

$$g_{m3} = \frac{2.03}{0.026} = 78.08 \text{ mA/V}$$



$$V_i = V_{\pi 1} + V_{e1} \Rightarrow V_{e1} = V_i - V_{\pi 1} \quad (1)$$

$$\frac{V_{\pi 1}}{r_{\pi 1}} + g_{m1} V_{\pi 1} = V_{\pi 1} (35.18) = \frac{V_{e1}}{R_{E1}} + \frac{V_{e1} - V_0}{R_F} = (V_i - V_{\pi 1}) \left(\frac{1}{0.5} + \frac{1}{10} \right) - \frac{V_0}{10} = V_i (2.10) - V_0 (0.10) \quad (2)$$

$$V_{\pi 2} = -(g_{m1} V_{\pi 1})(R_{C1} \parallel r_{\pi 2}) = -(32.81) V_{\pi 1} (88 \parallel 6.28) = -V_{\pi 1} (120.2) \quad (3)$$

$$g_{m2} V_{\pi 2} + \frac{V_{\pi 3} + V_0}{R_{C2}} + \frac{V_{\pi 3}}{r_{\pi 3}} = V_{\pi 2} (19.12) + V_{\pi 3} (0.7263) + V_0 (0.07692) = 0 \quad (4)$$

$$\frac{V_{\pi 3}}{r_{\pi 3}} + g_{m3} V_{\pi 3} = V_{\pi 3} (78.73) = \frac{V_0}{R_{E3}} + \frac{V_0 - V_{e1}}{R_F} = V_0 (0.8143) - V_i (0.10) + V_{\pi 1} (0.10) \quad (5)$$

Now substituting $V_{\pi 2} = -V_{\pi 1} (120.2)$ in (4):

$$(19.12)[-V_{\pi 1} (120.2)] + V_{\pi 3} (0.7263) + V_0 (0.07692) = 0$$

$$-V_{\pi 1} (2298.2) + V_{\pi 3} (0.7263) + V_0 (0.07692) = 0 \quad \text{Then} \quad V_{\pi 3} = V_{\pi 1} (3164.3) - V_0 (0.1059)$$

Substituting $V_{\pi 3} = V_{\pi 1} (3164.3) - V_0 (0.1059)$ in (5):

$$(78.73)[V_{\pi 1} (3164.3) - V_0 (0.1059)] = V_0 (0.8143) - V_i (0.10) + V_{\pi 1} (0.10)$$

$$\text{or } V_{\pi 1} (2.49 \times 10^5) - V_0 (9.152) = -V_i (0.10)$$

$$\text{Then } V_{\pi 1} = V_0 (3.674 \times 10^{-5}) - V_i (4.014 \times 10^{-7})$$

$$\text{in (2): } (35.18)[V_0 (3.674 \times 10^{-5}) - V_i (4.014 \times 10^{-7})]$$

$$\text{Now substituting } V_{\pi 1} = V_0 (3.674 \times 10^{-5}) - V_i (4.014 \times 10^{-7})$$

$$\text{or } V_0 (0.1013) = V_i (2.10) \quad \text{So } \frac{V_0}{V_i} = 20.7$$

c. $R_{\text{eff}} = \frac{V_i}{I_i}$ and $I_i = I_{R_{B1}} + I_{b1}$

$$I_{R_{B1}} = \frac{V_i}{R_{B1}} \quad I_{b1} = \frac{V_{\pi 1}}{r_{\pi 1}}$$

$$V_{\pi 1} = (20.7V_i)(3.674 \times 10^{-5}) - V_i(4.014 \times 10^{-7}) \\ = V_i(7.60 \times 10^{-4})$$

Then

$$R_{\text{eff}} = \frac{V_i}{\frac{V_i}{63.2} + \frac{V_i(7.60 \times 10^{-4})}{3.66}} \\ = \frac{1}{0.01582 + 2.077 \times 10^{-4}} = \underline{\underline{62.4 \text{ k}\Omega}}$$

d. $V_i = 0$ Equation (1) is modified to $V_{\pi 1} + V_{e1} = 0$

Equation (5) is modified to:

$$V_{\pi 3}(78.73) + I_X = V_0(0.8143) + V_{\pi 1}(0.10) \quad (5)$$

Now

$$V_{\pi 1}(35.18) = -V_0(0.10) \quad (2)$$

$$V_{\pi 2} = -V_{\pi 1}(120.2) \quad (3)$$

$$V_{\pi 2}(19.12) + V_{\pi 3}(0.7263) + V_0(0.07692) = 0 \quad (4)$$

Now

$$V_{\pi 1} = -V_0(0.002843)$$

so

$$V_{\pi 2} = -(-V_0)(0.002843)(120.2)$$

$$V_{\pi 2} = V_0(0.3417)$$

Then

$$V_0(0.3417)(19.12) + V_{\pi 3} + (0.7263) + V_0(0.07692) = 0$$

$$\text{or } V_{\pi 3} = -V_0(9.101) \quad (4)$$

So then

$$-V_0(9.101)(78.73) + I_X$$

$$= V_0(0.8143) + (0.10)(-V_0)(0.002843)$$

or

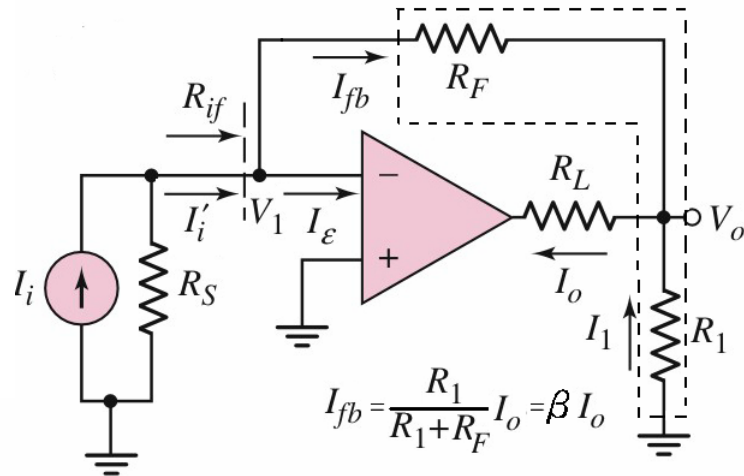
$$I_X = V_0(717.3) \quad (5)$$

or

$$R_{0f} = \frac{V_0}{I_X} = 0.00139 \text{ k}\Omega \Rightarrow \underline{\underline{R_{0f} = 1.39 \Omega}}$$

第十二章 回授與穩定度

12.5 並-串回授組態



$$I_i \cong I_i = I_{fb}$$

$$V_o = -I_{fb} R_F = -I_i R_F$$

$$I_o = I_{fb} + I_1 = I_i + \left(-\frac{1}{R_1}\right)(-I_i R_F) = I_i \left(1 + \frac{R_F}{R_1}\right)$$

$$\frac{I_o}{I_i} = 1 + \frac{R_F}{R_1}$$

$$A_{if} = \frac{I_o}{I_i} = \frac{1}{\beta_i}$$

$$\beta_i = \frac{1}{1 + \frac{R_F}{R_1}}$$

就有限放大增益而言

$$I_o = A_i I_\epsilon$$

$$I_\epsilon = I_i - I_{fb} \cong I_i - I_{fb}$$

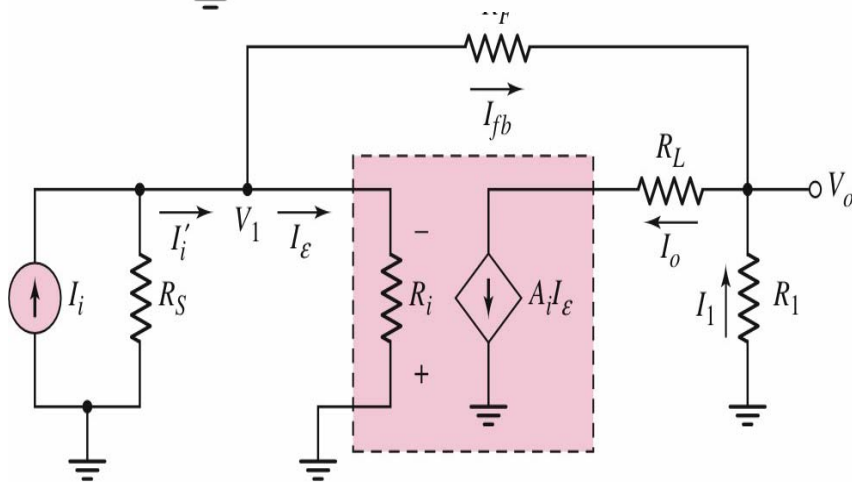
$$I_o = A_i (I_i - I_{fb})$$

$$V_o = -I_{fb} R_F$$

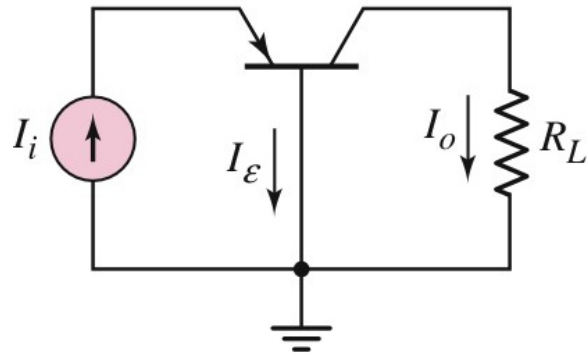
$$I_1 = -\frac{V_o}{R_1} = -\left(\frac{1}{R_1}\right)(-I_{fb} R_F) = I_{fb} \left(\frac{R_F}{R_1}\right)$$

$$I_o = I_{fb} + I_1 = I_{fb} + I_{fb} \left(\frac{R_F}{R_1}\right)$$

$$A_{if} = \frac{I_o}{I_i} = \frac{A_i}{1 + \frac{A_i R_F}{R_1}}$$



第十二章 回授與穩定度



(a)

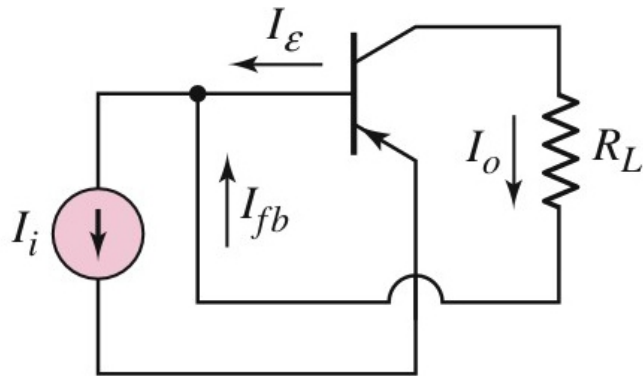
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基本放大增益為

$$I_o / I_\varepsilon = A_i = h_{FE}$$

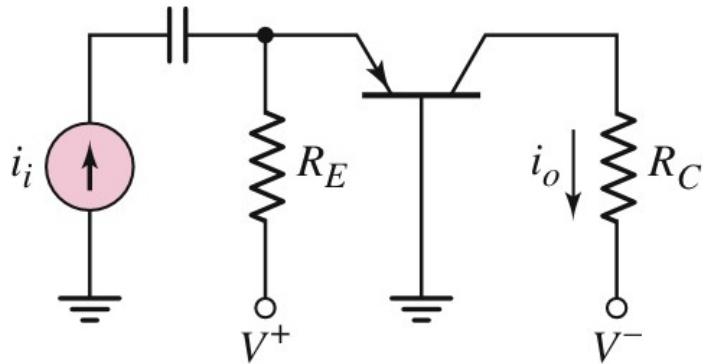
閉迴路電流轉換方程式或增益可表示為

$$A_{if} = \frac{I_o}{I_i} = \frac{h_{FE}}{1 + h_{FE}} = \frac{A_i}{1 + A_i}$$



(b)

第十二章 回授與穩定度

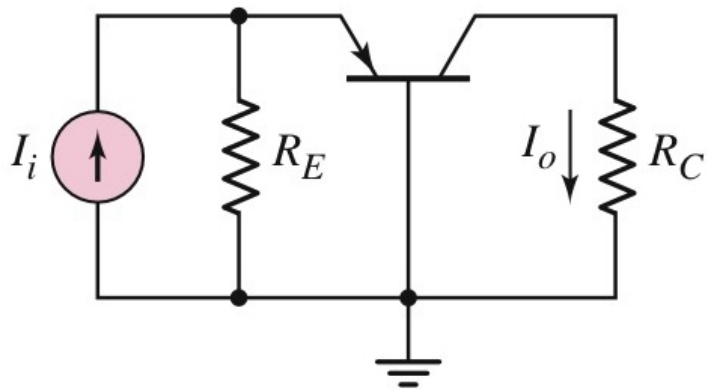


(a)

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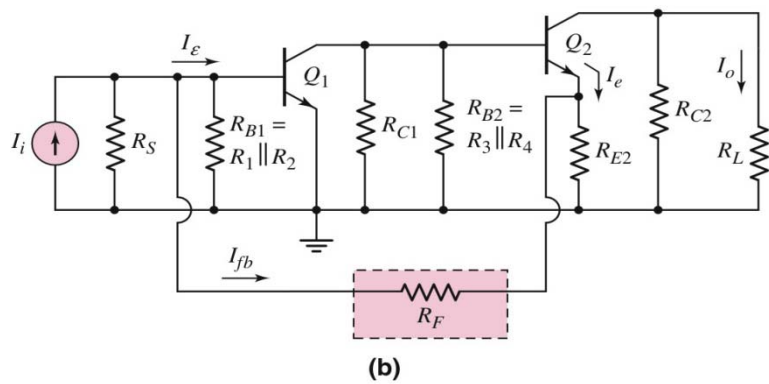
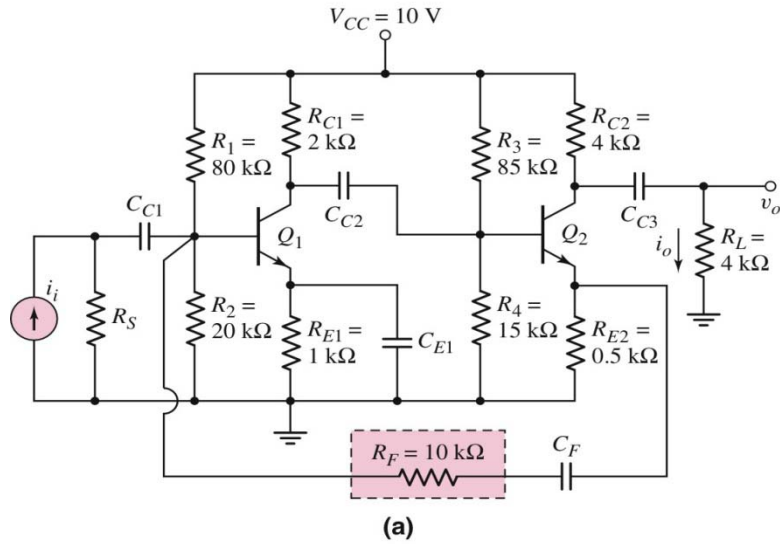
圖(a)中為更實際的共基極電流增益電路

$$A_{if} = \frac{I_o}{I_i} = \frac{h_{FE}}{\left(1 + \frac{r_\pi}{R_E}\right) + h_{FE}} = \frac{A_i}{\left(1 + \frac{r_\pi}{R_E}\right) + A_i}$$



(b)

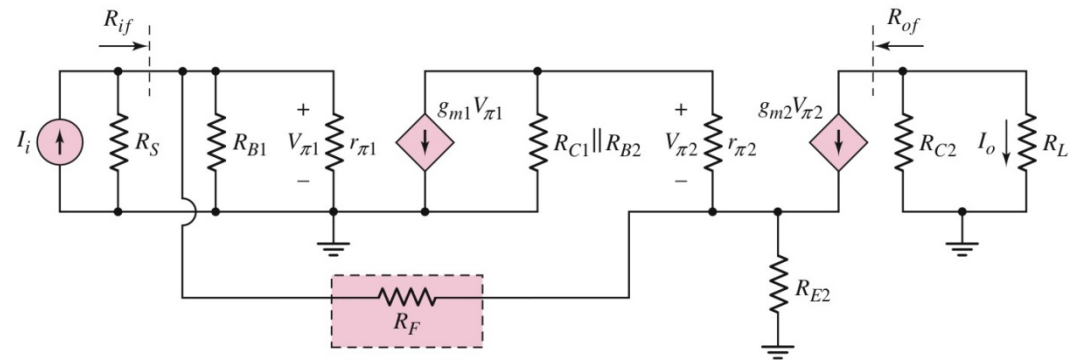
第十二章 回授與穩定度



圖(a)為離散電晶體並-串回授電路的例子；
圖(b)為交流等效電路。

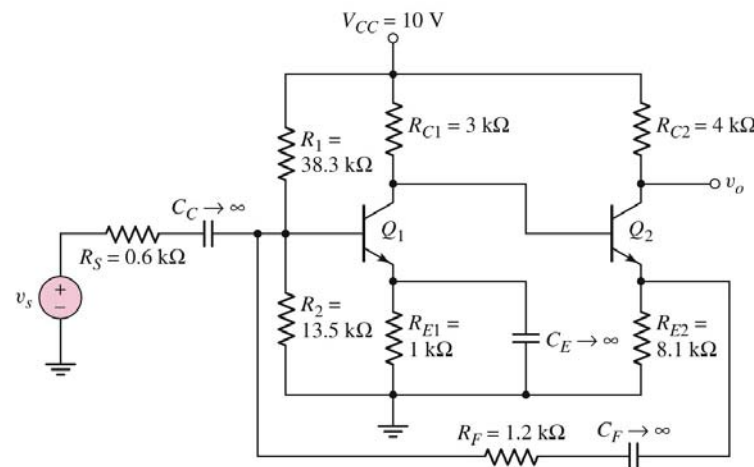
其中負載電流 I_o 及回授電流 I_{fb} 正比於射極電流 I_e 。

下圖為小信號等效電路。



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12.46 The circuit in Figure P12.46 is an example of a shunt-series feedback circuit. A signal proportional to the output current is fed back to the shunt connection at the base of Q_1 . However, the circuit may be used as a voltage amplifier. Assume transistor parameter of $h_{FE}=120$, $V_{BE(on)}=0.7V$, and $V_A=\infty$. (a) Determine the small-signal parameters for Q_1 and Q_2 . (b) Using nodal analysis, determine the small-signal voltage gain $A_V=v_o/v_s$.



$$\text{a. } R_{TH} = 13.5 \parallel 38.3 = 9.98 \text{ k}\Omega \quad V_{TH} = \left(\frac{13.5}{13.5 + 38.3} \right) (10) = 2.606 \text{ V}$$

$$I_{C1} = \frac{(120)(2.606 - 0.7)}{9.98 + (121)(1)} = 1.75 \text{ mA} \quad V_{C1} = 10 - (1.75)(3) = 4.75 \text{ V}$$

$$I_{C2} \approx \frac{4.75 - 0.7}{8.1} = 0.50 \text{ mA}$$

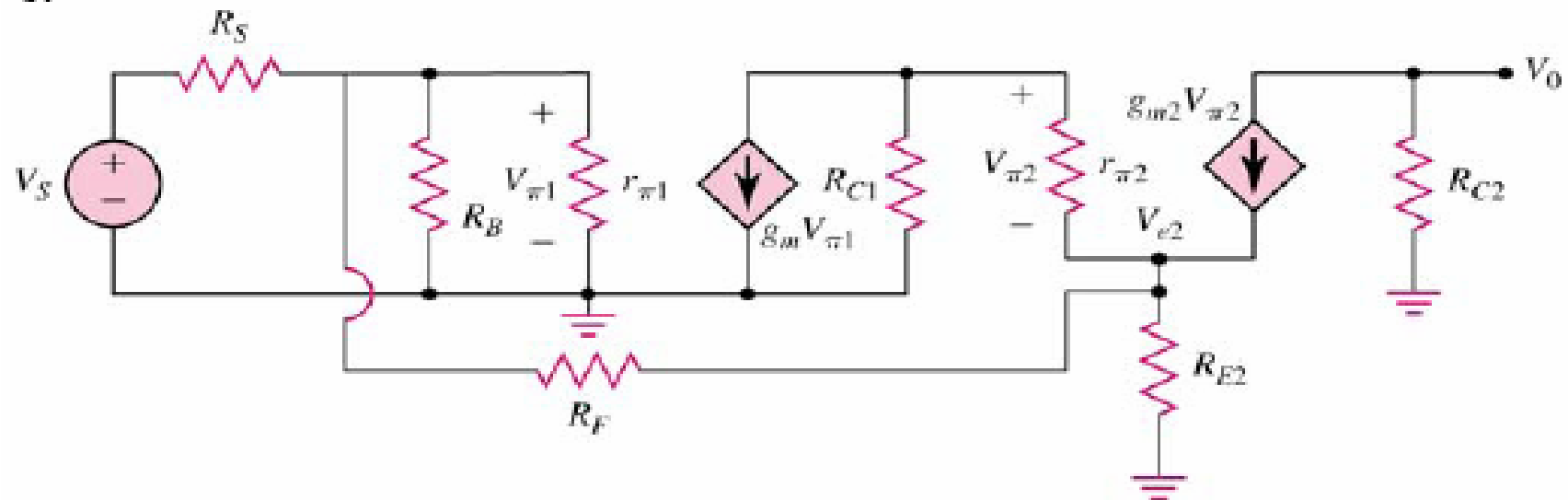
$$r_{\pi 1} = \frac{(120)(0.026)}{1.75} = 1.78 \text{ k}\Omega$$

$$g_{m1} = \frac{1.75}{0.026} = 67.31 \text{ mA/V}$$

$$r_{\pi 2} = \frac{(120)(0.026)}{0.50} = 6.24 \text{ k}\Omega$$

$$g_{m2} = \frac{0.50}{0.026} = 19.23 \text{ mA/V}$$

b.



$$\frac{V_S - V_{\pi 1}}{R_S} = \frac{V_{\pi 1}}{R_B \parallel r_{\pi 1}} + \frac{V_{\pi 1} - V_{e 2}}{R_F} \quad (1)$$

$$g_{m1} V_{\pi 1} + \frac{V_{\pi 2} + V_{e 2}}{R_{C1}} + \frac{V_{\pi 2}}{r_{\pi 2}} = 0 \quad (2)$$

$$\frac{V_{\pi 2}}{r_{\pi 2}} + g_{m2} V_{\pi 2} = \frac{V_{e 2}}{R_{E2}} + \frac{V_{e 2} - V_{\pi 1}}{R_F} \quad (3)$$

$$\text{and } V_0 = -(g_{m2} V_{\pi 2}) R_{C2} \quad (4)$$

Substitute numerical values in (1), (2), and (3)

$$\frac{V_S}{0.6} = V_{\pi 1} \left[\frac{1}{0.6} + \frac{V_{\pi 1}}{9.98 \parallel 1.78} + \frac{1}{1.2} \right] - \frac{V_{e 2}}{1.2}$$

$$V_S(1.67) = V_{\pi 1}(4.011) - V_{e 2}(0.8333) \quad (1)$$

$$(67.31)V_{\pi 1} + V_{\pi 2} \left(\frac{1}{3} + \frac{1}{6.24} \right) + \frac{V_{e 2}}{3} = 0$$

$$V_{\pi 1}(67.31) + V_{\pi 2}(0.4936) + V_{e 2}(0.3333) = 0 \quad (2)$$

$$V_{\pi 1} \left(\frac{1}{6.24} + 19.23 \right) = \frac{V_{e 2}}{8.1} + \frac{V_{e 2}}{1.2} - \frac{V_{\pi 2}}{1.2}$$

$$V_{\pi 2}(19.39) = V_{e 2}(0.9568) - V_{\pi 1}(0.8333) \quad (3)$$

From (1)

$$V_{e 2} = V_{\pi 1}(4.813) - V_S(2.00)$$

Then

$$V_{\pi 1}(67.31) + V_{\pi 2}(0.4936) + (0.3333)[V_{\pi 1}(4.813) - V_S(2.00)] = 0$$

or

$$V_{\pi 1}(68.91) + V_{\pi 2}(0.4936) - V_S(0.6666) = 0 \quad (2')$$

and

$$V_{\pi 2}(19.39) = (0.9568)[V_{\pi 1}(4.813) - V_S(2.00)] - V_{\pi 1}(0.8333)$$

or

$$V_{\pi 2}(19.39) = V_{\pi 1}(3.772) - V_S(1.914) \quad (3')$$

We find

$$V_{\pi 1} = V_S(0.009673) - V_{\pi 2}(0.007163)$$

Then

$$V_{\pi 2}(19.39) = (3.772)[V_S(0.009673) - V_{\pi 2}(0.007163)] - V_S(1.914)$$

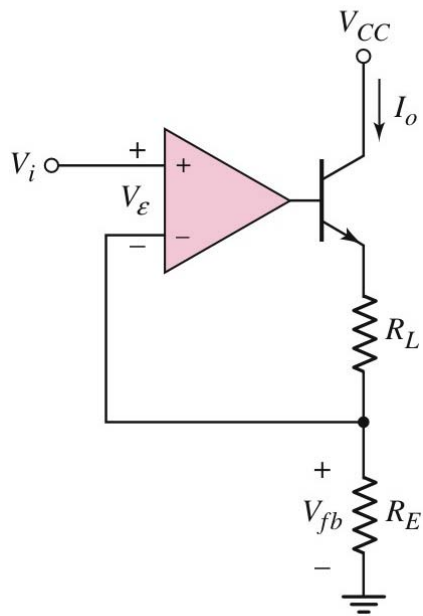
$$V_{\pi 2}(19.42) = V_S(-1.878) \text{ or } V_{\pi 2} = -V_S(0.09670)$$

$$\text{so that } V_0 = -(19.23)(4)(-V_S)(0.09670)$$

$$\text{Then } \frac{V_0}{V_S} = 7.44$$

第十二章 回授與穩定度

12.6 串-串回授組態



$$A_{gf} = \frac{I_o}{V_i} \cong \frac{1}{\beta_z}$$

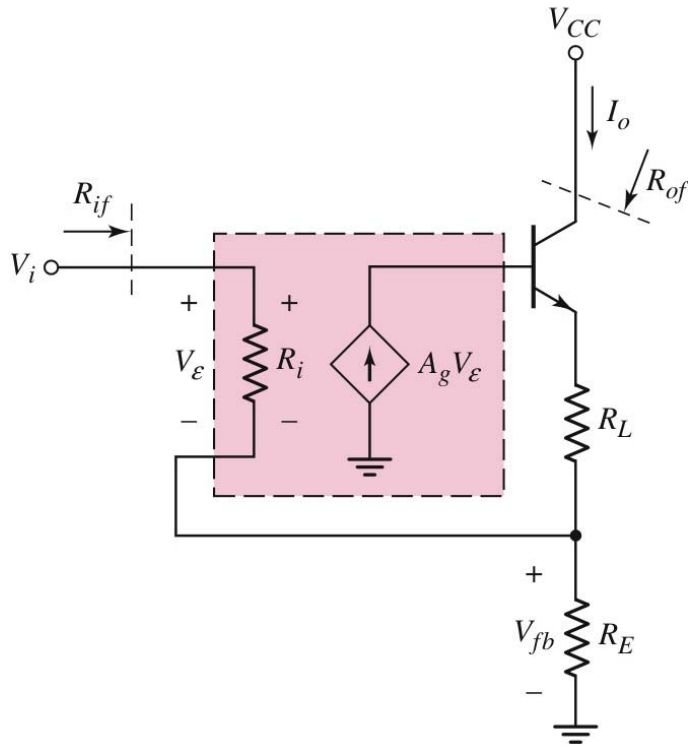
考慮放大器電路為理想的並忽略電晶體之基極電流

$$V_i = V_{fb} = I_o R_E$$

$$A_{gf} = \frac{I_o}{V_i} = \frac{1}{R_E}$$

$$\beta_z = R_E$$

第十二章 回授與穩定度



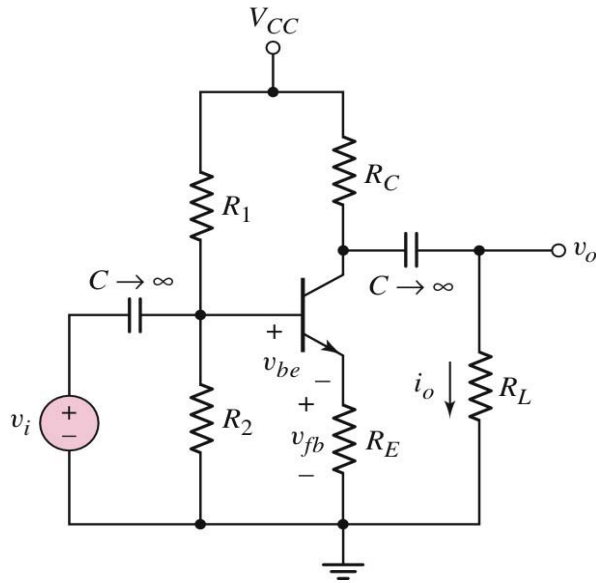
$$I_o = \frac{V_{fb}}{R_E} = h_{FE} I_b = h_{FE} A_g V_\varepsilon$$

$$V_\varepsilon = V_i - V_{fb} = V_i - I_o R_E$$

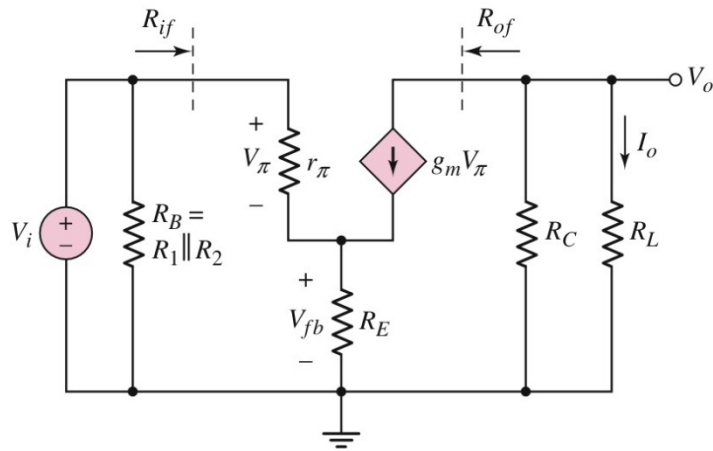
$$I_o = h_{FE} A_g (V_i - I_o R_E)$$

$$A_{gf} = \frac{I_o}{V_i} = \frac{(h_{FE} A_g)}{1 + (h_{FE} A_g) R_E}$$

第十二章 回授與穩定度



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$$I_o = - (g_m V_\pi) \left(\frac{R_C}{R_C + R_L} \right)$$

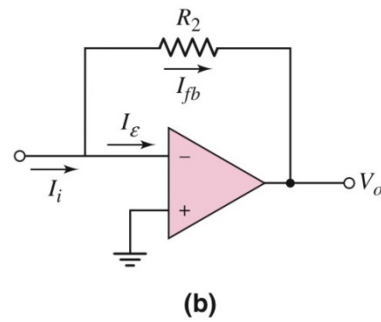
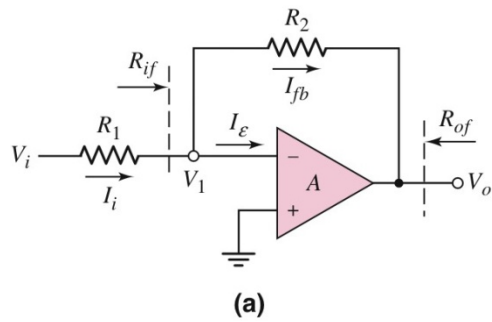
$$V_{fb} = \left(\frac{V_\pi}{r_\pi} + g_m V_\pi \right) R_E$$

$$V_i = V_\pi + V_{fb} = V_\pi \left[1 + \left(\frac{1}{r_\pi} + g_m \right) R_E \right]$$

$$A_{gf} = \frac{I_o}{V_i} = \frac{-g_m \left(\frac{R_C}{R_C + R_L} \right)}{1 + \left(\frac{1}{r_\pi} + g_m \right) R_E}$$

第十二章 回授與穩定度

12.7 並-並回授組態



$$A_{zf} = \frac{V_o}{I_i} \cong \frac{1}{\beta_g}$$

$$V_o = -I_{fb}R_2$$

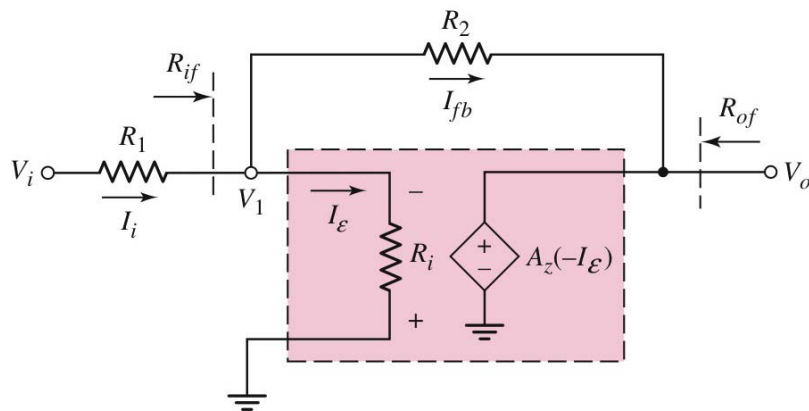
$$I_{fb} = I_i \rightarrow A_{zf} = \frac{V_o}{I_i} = -R_2$$

$$\beta_g = -\frac{1}{R_2}$$

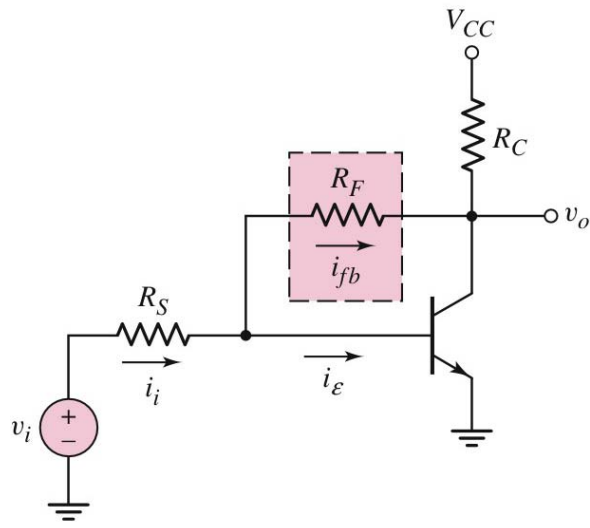
$$V_o = -A_z I_\epsilon, \quad I_\epsilon = I_i - I_{fb}, \quad V_o = -A_z (I_i - I_{fb})$$

$$\rightarrow I_{fb} = -V_o / R_2$$

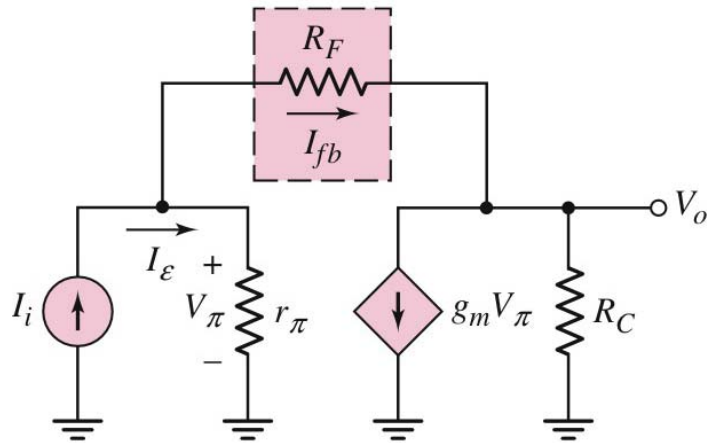
$$A_{zf} = \frac{V_o}{I_i} = \frac{-A_z}{\left(1 + \frac{A_z}{R_2}\right)} = \frac{-A_z}{1 + (-A_z)\beta_g}$$



第十二章 回授與穩定度



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$$\frac{V_o}{R_c} + g_m V_\pi + \frac{V_o - V_\pi}{R_F} = 0$$

$$I_i = \frac{V_\pi}{R_\pi} + \frac{V_\pi - V_o}{R_F}$$

$$V_o \left(\frac{1}{R_C} + \frac{1}{R_F} \right) \left(\frac{1}{r_\pi} + \frac{1}{R_F} \right) + \left(g_m - \frac{1}{R_F} \right) \left(I_i + \frac{V_o}{R_F} \right) = 0$$

$$A_{zf} = \frac{V_o}{I_i} = \frac{- \left(g_m - \frac{1}{R_F} \right)}{\left(\frac{1}{R_C} + \frac{1}{R_F} \right) \left(\frac{1}{r_\pi} + \frac{1}{R_F} \right) + \frac{1}{R_F} \left(g_m - \frac{1}{R_F} \right)}$$

$$A_z = \frac{-g_m}{\left(\frac{1}{R_C} \right) \left(\frac{1}{r_\pi} \right)} = -g_m r_\pi R_C = -h_{FE} R_C$$

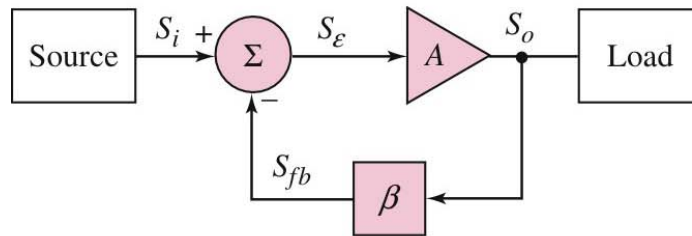
$$A_{zf} = \frac{V_o}{I_i} = \frac{+ \left(A_z + \frac{r_\pi R_C}{R_F} \right)}{\left(1 + \frac{R_C}{R_F} \right) \left(1 + \frac{r_\pi}{R_F} \right) - \frac{1}{R_F} \left(A_z + \frac{r_\pi R_C}{R_F} \right)}$$

$$h_{FE} = g_m r_\pi \gg r_\pi / R_F, \quad R_C \ll R_F, \quad r_\pi \ll R_F$$

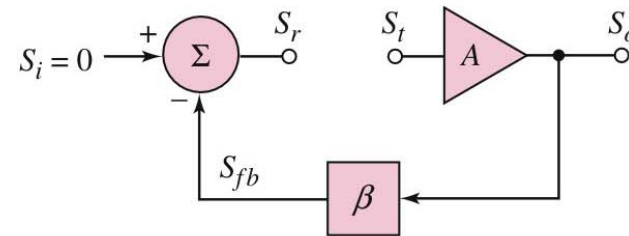
$$A_{zf} = \frac{V_o}{I_i} = \frac{A_z}{1 + (A_z) \left(\frac{-1}{R_F} \right)} \rightarrow \beta_g \cong \frac{-1}{R_F}$$

第十二章 回授與穩定度

12.8 迴路增益



(a)



(b)

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迴路增益推導：

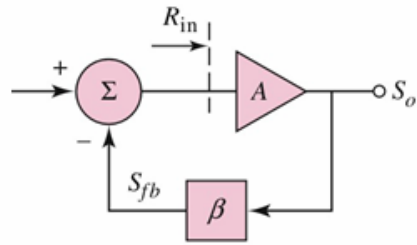
1. $S_i = 0$
2. 切斷迴路
3. 推導迴路增益

$$S_{fb} = \beta S_o = A\beta S_t$$

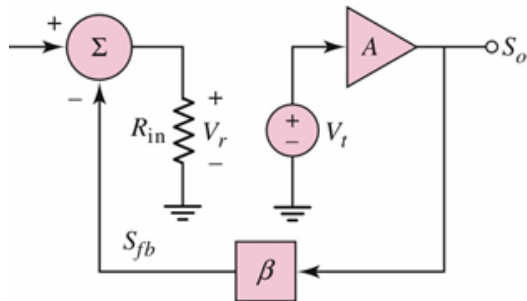
$$\frac{S_r}{S_t} = -A\beta$$

第十二章 回授與穩定度

考慮切斷迴路之影響



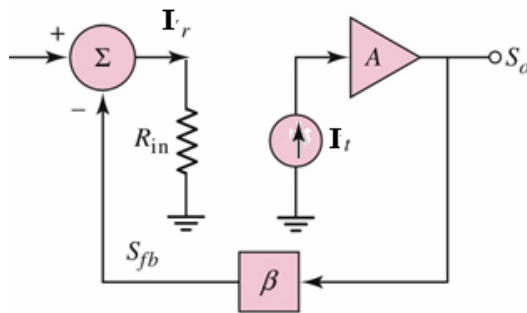
(a)



(b)

$$T = A\beta = -\frac{V_r}{V_t}$$

或

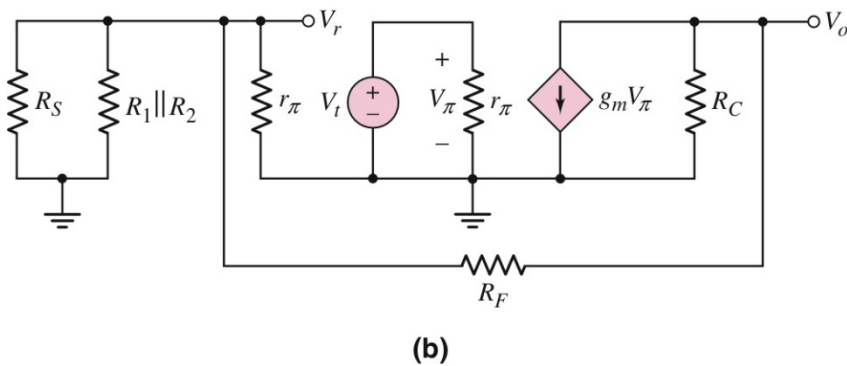
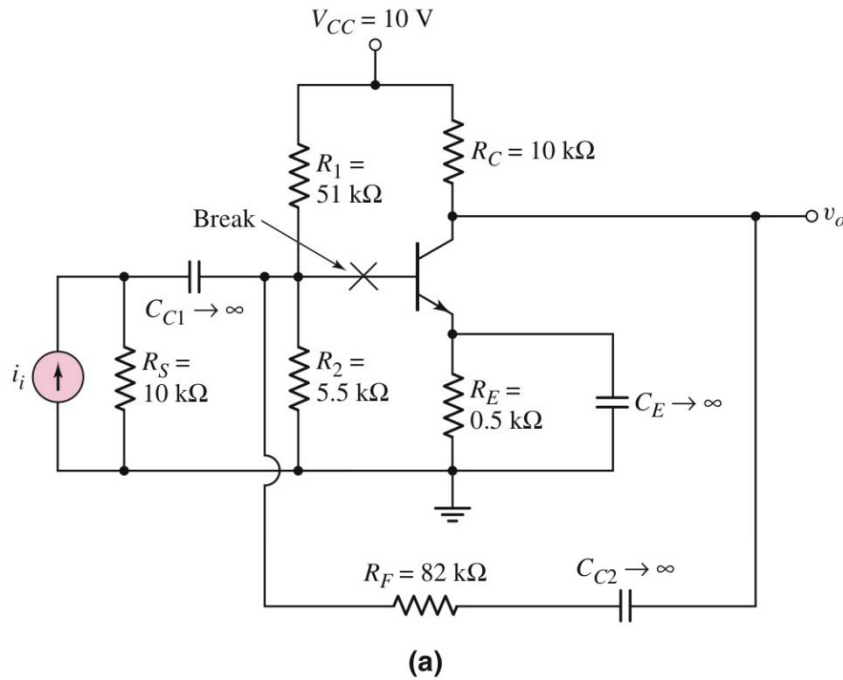


(c)

$$T = A\beta = -\frac{I_r}{I_t}$$

第十二章 回授與穩定度

例：



$$I_r \rightarrow V_r = I_r r_\pi; \quad I_t \rightarrow V_t = I_t r_\pi$$

$$T = A\beta = -\frac{I_r}{I_t} = -\frac{V_r}{V_t}$$

$$V_o = -g_m V_t [R_C \parallel (R_F + R_{eq})]$$

$$V_r = \left[\frac{R_{eq}}{R_F + R_{eq}} \right] V_o$$

$$T = -\frac{V_r}{V_t} = +g_m \left[\frac{R_{eq}}{R_F + R_{eq}} \right] [R_C \parallel (R_F + R_{eq})]$$

$$R_{eq} = R_S \parallel R_1 \parallel R_2 \parallel r_\pi$$

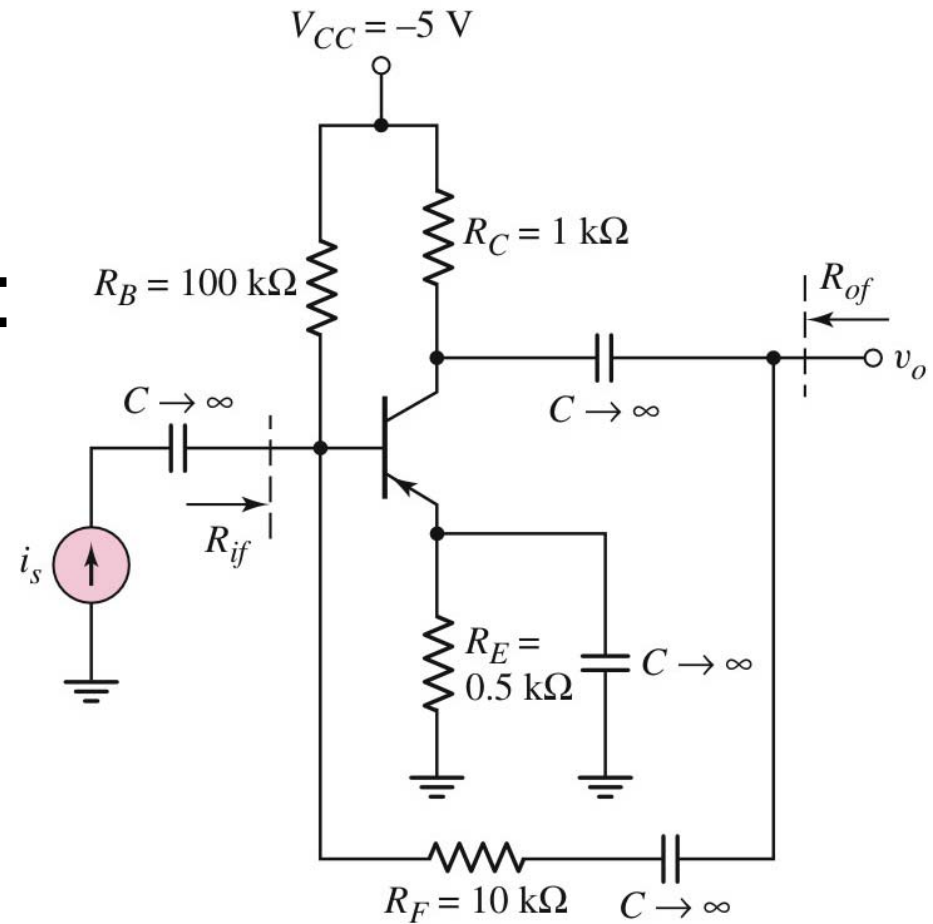
$$T = (g_m R_C) \left(\frac{R_{eq}}{R_C + R_F + R_{eq}} \right)$$

The transistor parameters for the (transresistance amplifier) circuit are:

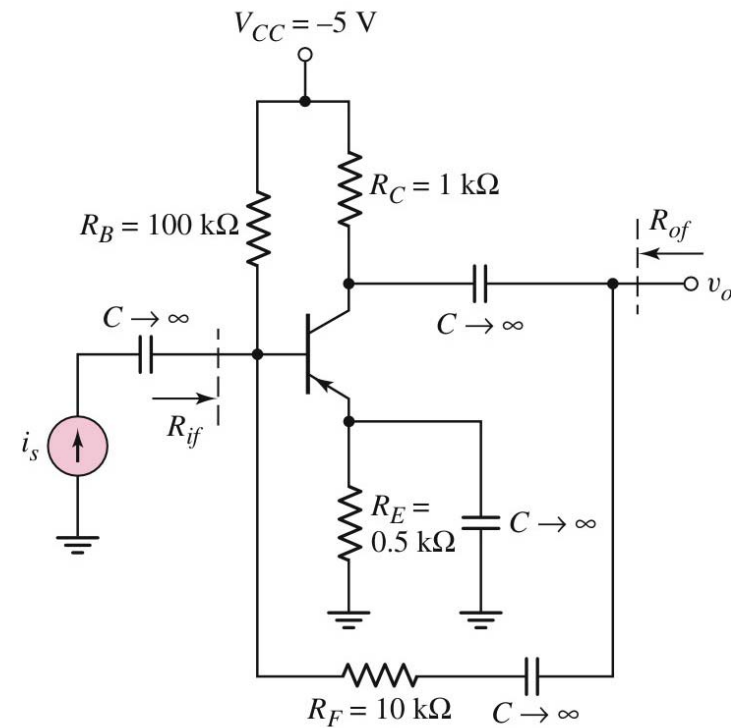
$$h_{FE} = 80, V_{EB} = 0.7V, \text{ and } V_A = 100V.$$

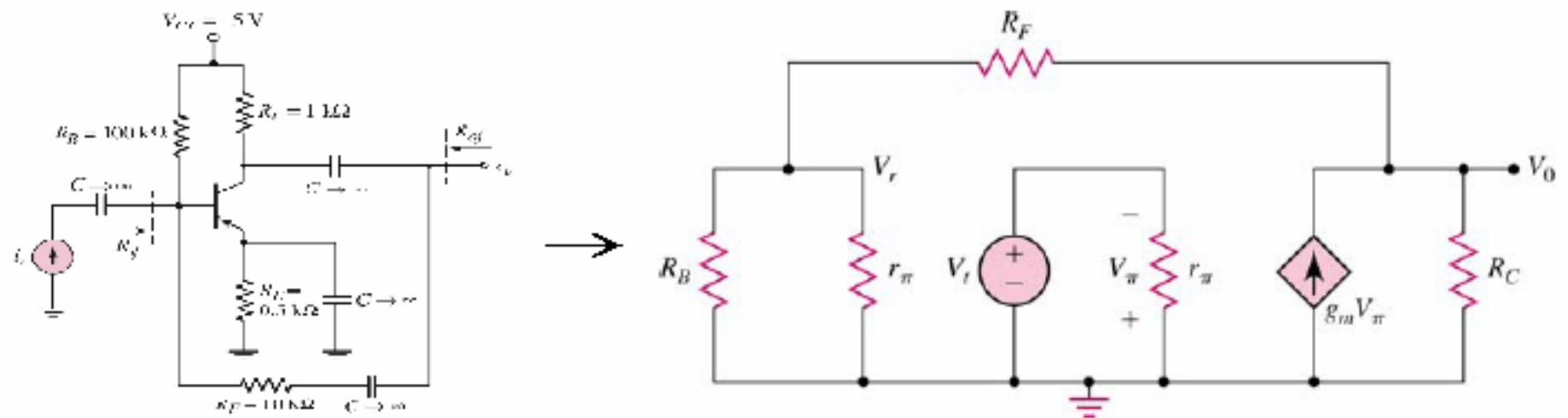
Find the loop gain T .

(Calculate r_{π} , g_m , and then T)



12.64 The transistor parameters for the circuit shown in Figure P12.54 are:
 $\rightarrow h_{FE} = 50$, $V_{BE} = 0.7V$, and $V_A = 100V$. Find the loop gain T .





dc analysis

$$I_E R_E + V_{EB}(\text{on}) + I_B R_B + V_{CC} = 0 \rightarrow I_B = \frac{5 - 0.7}{100 + (51)(0.5)} = 0.0343 ; I_C = (50)(0.0343) = 1.71 \text{ mA}$$

$$\text{Then } r_\pi = \frac{(50)(0.026)}{1.71} = 0.760 \text{ k}\Omega ; g_m = \frac{1.71}{0.026} = 65.77 \text{ mA/V}$$

$$V_\pi = -V_r$$

$$g_m V_\pi = \frac{V_o}{R_C} + \frac{V_o}{R_F + R_B \parallel r_\pi} \rightarrow (65.77)V_\pi = V_o \left(\frac{1}{1} + \frac{1}{10 + 100 \parallel 0.760} \right) = V_o (1.0930) \quad (1)$$

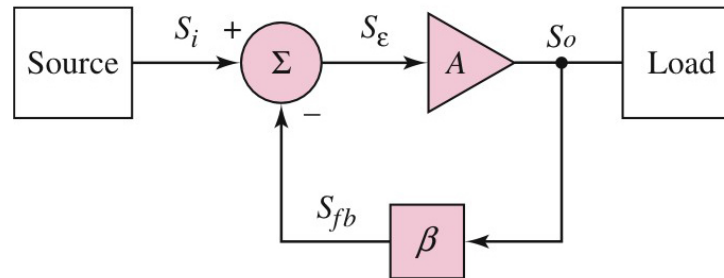
$$\text{and } V_r = \left(\frac{R_B \parallel r_\pi}{R_B \parallel r_\pi + R_F} \right) V_o = \left(\frac{0.754}{10 + 0.754} \right) V_o = (0.07011)V_o \rightarrow V_o = (14.26)V_r \quad (2)$$

$$\text{Then } (65.77)(-V_r) = (14.26)V_r (1.0930)$$

$$\frac{V_r}{V_r} = -4.22 \text{ so that } T = 4.22$$

第十二章 回授與穩定度

12.9 回授放大器之穩定性



$$A_f \equiv \frac{S_o}{S_i} = \frac{A}{1 + A\beta} = \frac{A}{1 + T}$$

$$\rightarrow A_f(j\omega) = \frac{A(j\omega)}{1 + T(j\omega)}; \quad T(j\omega) = A(j\omega)\beta(j\omega) = |T(j\omega)| \angle T(j\omega)$$

回授放大器之穩定性為迴路增益 **$T(j\omega)$** 之函數

回授放大器之穩定性：

- $T(j\omega) > -1$ 即 $\angle T(j\omega) = 180^\circ$ 時, $|T(j\omega)| < 1 \rightarrow$ 穩定 (放大器)
- $T(j\omega) \leq -1$ 即 $\angle T(j\omega) = 180^\circ$ 時, $|T(j\omega)| \geq 1 \rightarrow$ 不穩定 (振盪器)

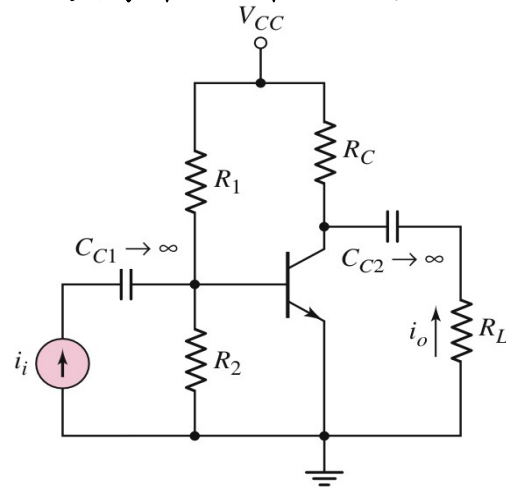
若回授電路為電阻性電路(即 $\beta(j\omega) = \beta$)

$\rightarrow \angle T(j\omega) = \angle A(j\omega)$

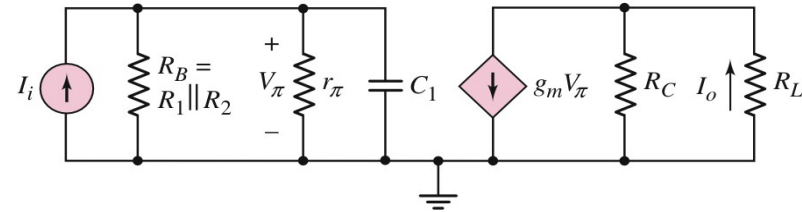
使用 **$T(j\omega)$** 的Blode plots判斷回授放大器之穩定性

第十二章 回授與穩定度

A. 放大器為簡單之單級共射極電流放大器



(a)



(b)

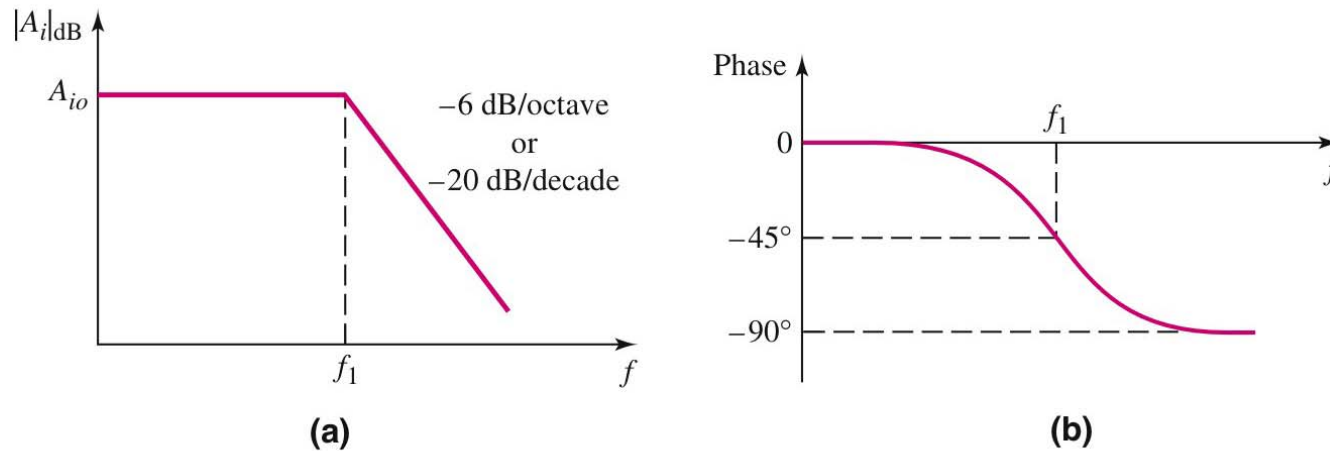
$$I_o = \left(\frac{R_C}{R_C + R_L} \right) g_m V_\pi \quad , \quad V_\pi = I_i \left[R_\pi \parallel \left(\frac{1}{sC_1} \right) \right] = I_i \left[\frac{R_\pi}{1 + sR_\pi C_1} \right]$$

where $R_\pi = r_\pi \parallel R_B = r_\pi \parallel R_1 \parallel R_2$

$$A_i = g_m R_\pi \left(\frac{R_C}{R_C + R_L} \right) \left[\frac{1}{1 + sR_\pi C_1} \right]$$

$$A_i = \frac{A_{io}}{1 + j \left(\frac{f}{f_1} \right)} = \frac{A_{io}}{\sqrt{1 + \left(\frac{f}{f_1} \right)^2}} \angle -\tan^{-1} \left(\frac{f}{f_1} \right)$$

第十二章 回授與穩定度



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圖 (a) 電流增益大小之波德圖

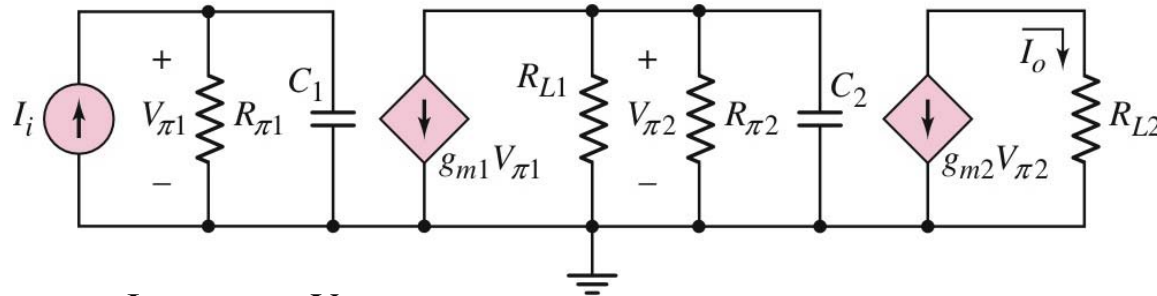
圖 (b) 電流增益相位之波德圖

低頻時，輸出電流與輸入電流同相

低頻時，輸出電流與輸入電流之相位差為 90°

第十二章 回授與穩定度

B. 放大器為二級放大器



二級放大器之
小信號等效電路

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$$V_{\pi 2} = -g_{m1} V_{\pi 1} \left[R_{L1} \parallel R_{L2} \parallel \left(\frac{1}{sC_2} \right) \right]$$

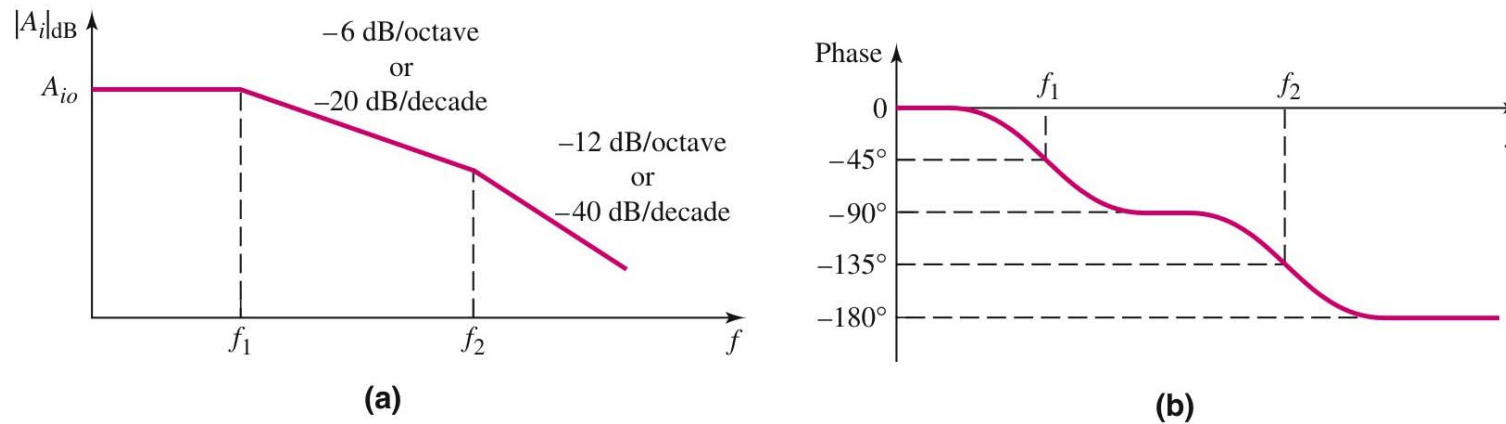
$$V_{\pi 1} = I_i \left[R_{\pi 1} \parallel \left(\frac{1}{sC_1} \right) \right]$$

$$A_i = \frac{I_o}{I_i} = (g_{m1} g_{m2}) (R_{\pi 1}) (R_{L1} \parallel R_{L2}) \left[\frac{1}{1 + sR_{\pi 1} C_1} \right] \left[\frac{1}{1 + s(R_{L1} \parallel R_{L2}) C_2} \right]$$

$$A_i = \frac{A_{io}}{\left(1 + j \frac{f}{f_1} \right) \left(1 + j \frac{f}{f_2} \right)}$$

$$A_i = \frac{A_{io}}{\sqrt{1 + \left(\frac{f}{f_1} \right)^2} \sqrt{1 + \left(\frac{f}{f_2} \right)^2}} \angle - \left[\tan^{-1} \left(\frac{f}{f_1} \right) + \tan^{-1} \left(\frac{f}{f_2} \right) \right]$$

第十二章 回授與穩定度



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圖 (a) 電流增益大小之波德圖

圖 (b) 電流增益相位之波德圖

低頻時，輸出電流與輸入電流同相

低頻時，輸出電流與輸入電流之相位差為 180°

第十二章 回授與穩定度

C. 放大器三級放大器

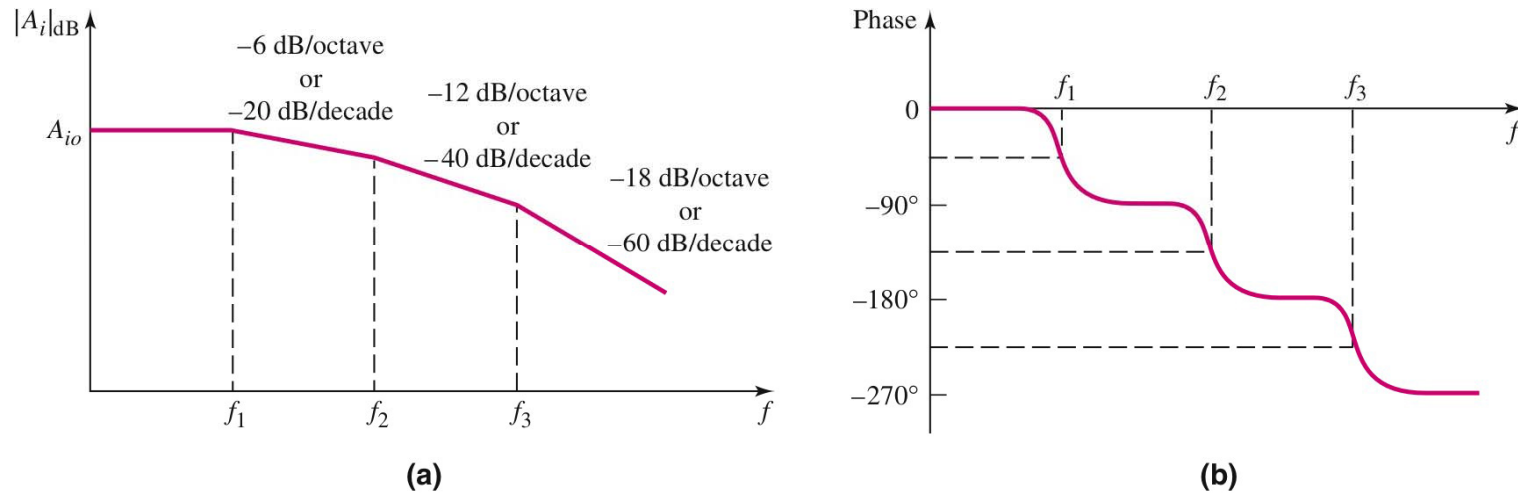


$$A = \frac{A_o}{\left(1 + j\frac{f}{f_1}\right)\left(1 + j\frac{f}{f_2}\right)\left(1 + j\frac{f}{f_3}\right)}$$

$$T(j\omega) = \beta A(j\omega)$$

$$T(f) = \frac{\beta A_o}{\left(1 + j\frac{f}{f_1}\right)\left(1 + j\frac{f}{f_2}\right)\left(1 + j\frac{f}{f_3}\right)}$$

第十二章 回授與穩定度



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圖 (a) 電流增益大小之波德圖

圖 (b) 電流增益相位之波德圖

低頻時，輸出電流與輸入電流同相

低頻時，輸出電流與輸入電流之相角差為 -270°

第十二章 回授與穩定度

例： $A(f) = \frac{(100)}{\left(1 + j\frac{f}{10^5}\right)^3}$; $\beta = 0.2$ 及 0.02

$$\rightarrow T(f) = \frac{\beta(100)}{\left(1 + j\frac{f}{10^5}\right)^3} = \frac{\beta(100)}{\left(\sqrt{1 + \frac{f}{10^5}}\right)^3} \angle -3 \tan^{-1}\left(\frac{f}{10^5}\right)$$

相位： $-3 \tan^{-1}\left(\frac{f_{180}}{10^5}\right) = -180^\circ$

\rightarrow -180度相位變之頻率 $f_{180} = 1.73 \times 10^5$ Hz

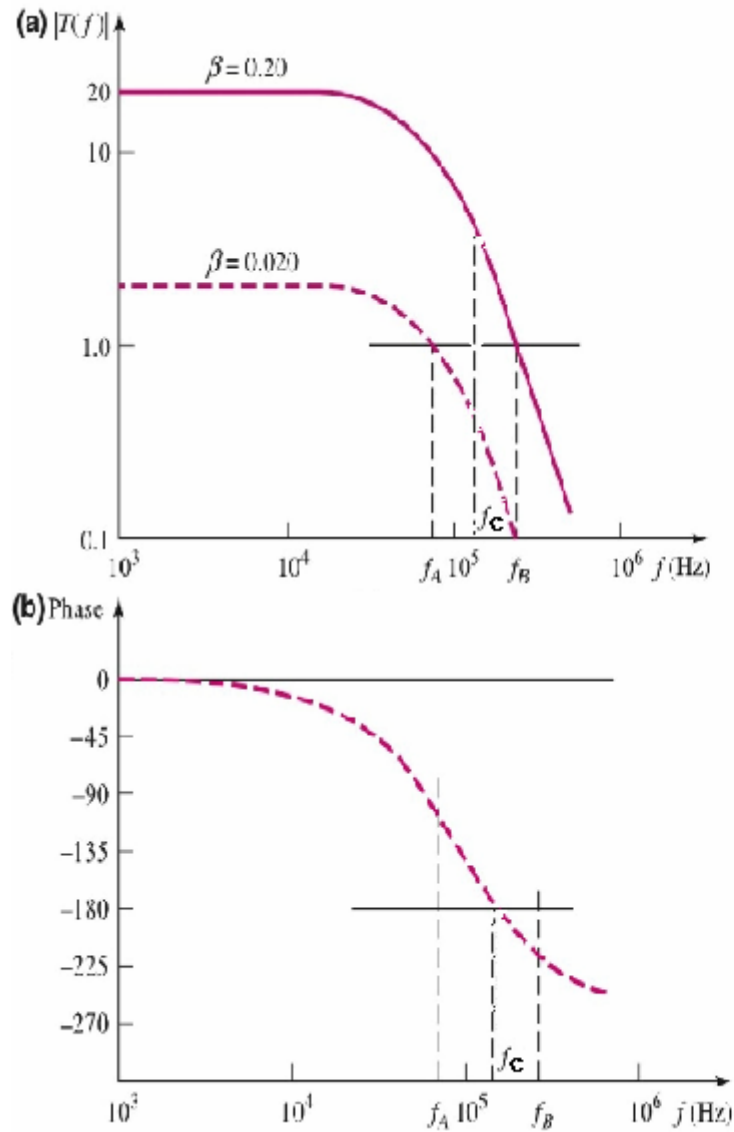
A. $\beta = 0.2$

$$|T(f_{180})| = \frac{(0.2)(100)}{8} = 2.5 \rightarrow \text{不穩定}$$

B. $\beta = 0.02$

$$|T(f_{180})| = \frac{(0.02)(100)}{8} = 0.25 \rightarrow \text{穩定}$$

第十二章 回授與穩定度



Bode Plots

A. $\beta = 0.02$

$$|T(f_A)| = 1; \angle T(f_A) > -180^\circ$$

→ 穩定

$$\text{即 } \angle T(f_C) = -180^\circ; |T(f_C)| < 1$$

B. $\beta = 0.2$

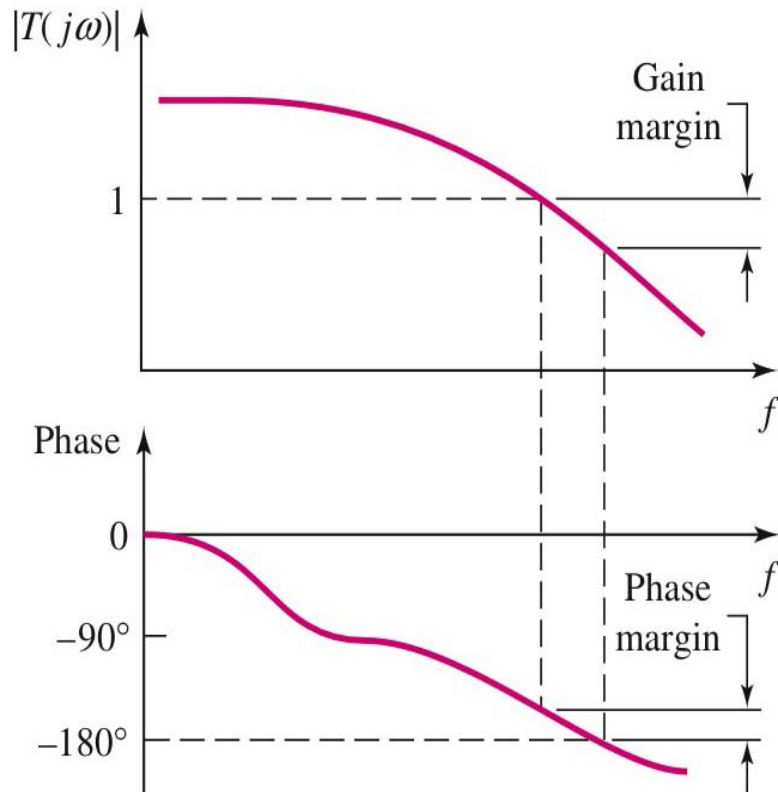
$$|T(f_B)| = 1; \angle T(f_B) < -180^\circ$$

→ 不穩定

$$\text{即 } \angle T(f_C) = -180^\circ; |T(f_C)| > 1$$

第十二章 回授與穩定度

相位邊限(phase margin)與增益邊限(gain margin):



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1. 增益邊限:

當 $\angle T(j\omega) = -180^\circ$ 操作頻率時，
若 $|T(j\omega)| < 1 \rightarrow$ 系統穩定

$$\begin{aligned} \text{增益邊限} &= 0 - |T(j\omega)| \text{ (dB)} \\ &= - |T(j\omega)| \text{ (dB)} \end{aligned}$$

2. 相位邊限:

當 $|T(j\omega)| = 1$ 操作頻率時，
若 $\angle T(j\omega) > -180^\circ \rightarrow$ 系統穩定

$$\begin{aligned} \text{相位邊限} &= \angle T(j\omega) - (-180^\circ) \\ &= \angle T(j\omega) + 180^\circ \end{aligned}$$

(典型所需之相位邊限落在45至60度)

12.66 The open-loop voltage gain of an amplifier is given by

$$A_v = \frac{10^3}{\left(1 + j \frac{f}{10^4}\right)^2 \left(1 + j \frac{f}{10^5}\right)}$$

- (a) Assuming the feedback transfer function is not a function of frequency, determine the frequency at which the phase of the loop gain is 180 degrees.
- (b) At what value of β will the feedback amplifier break into oscillation? (c) Using the value of β found in part (b), what is the low-frequency closed-loop gain? (d) Is the closed-loop feedback system stable for smaller or larger values of closed-loop gain?

$$(a) \quad T = \beta A_v = \frac{\beta(10^3)}{\left(1 + j \frac{f}{10^4}\right)^2 \left(1 + j \frac{f}{10^5}\right)}$$

$$\phi = -2 \tan^{-1} \frac{f}{10^4} - \tan^{-1} \frac{f}{10^5}$$

$$\text{Set } \phi = -180^\circ$$

By trial and error, $f = 4.58 \times 10^4$ Hz

$$(b) \quad \text{Set } |T| = 1 \text{ at } f = 4.58 \times 10^4 \text{ Hz}$$

$$1 = \frac{\beta(10^3)}{\left(\sqrt{1 + \left(\frac{4.58 \times 10^4}{10^4}\right)^2}\right)^2 \sqrt{1 + \left(\frac{4.58 \times 10^4}{10^5}\right)^2}}$$

$$1 = \frac{\beta(10^3)}{(21.976)(1.10)} \Rightarrow \beta = 0.02417$$

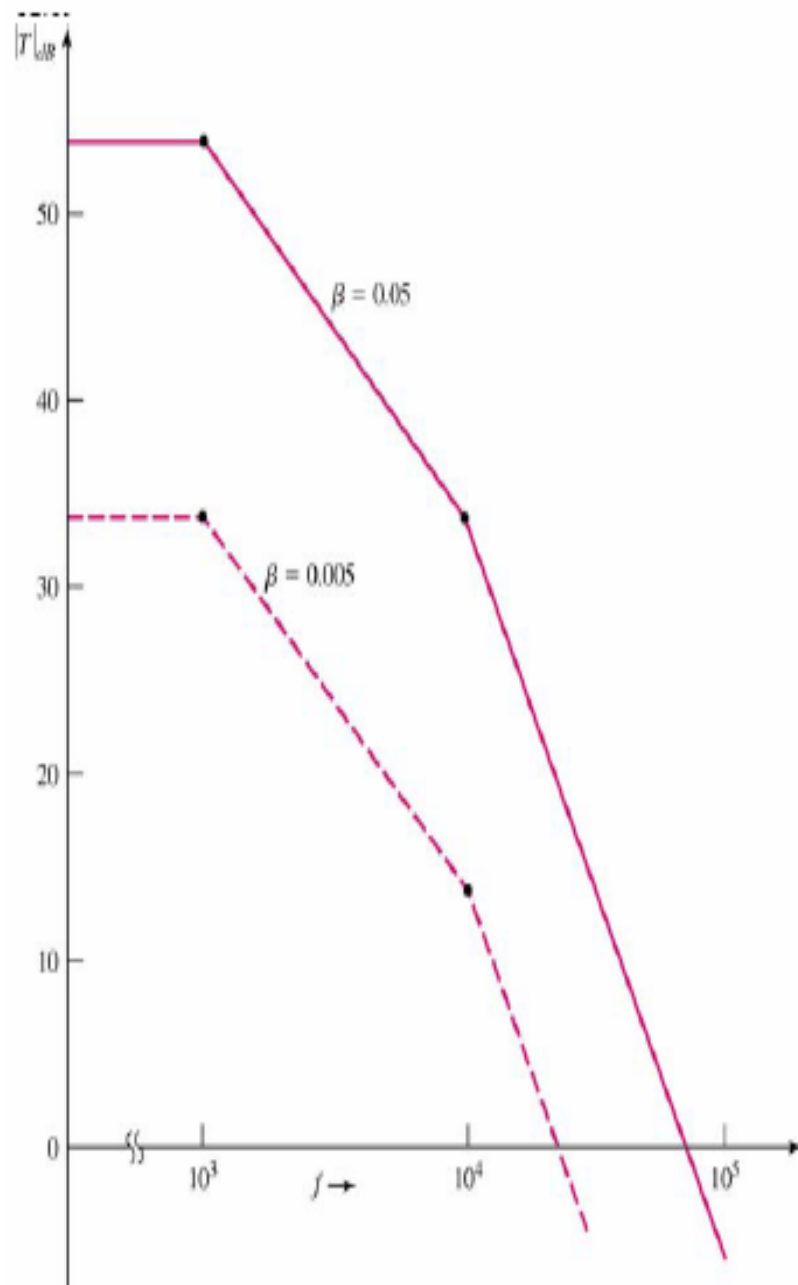
$$(c) \quad A_{v_o} = \frac{10^3}{1 + (10^3)(0.02417)} = 39.7$$

(d) Wait $|T| < 1$ at $f = 4.58 \times 10^4$ Hz, so system is stable for smaller values of β .

10.69 A three pole feedback amplifier has a loop gain given by

$$T(f) = \frac{\beta(10^4)}{\left(1 + j\frac{f}{10^3}\right)\left(1 + j\frac{f}{10^4}\right)\left(1 + j\frac{f}{10^5}\right)}$$

Sketch Bode Plots of the loop gain magnitude and phase for (a) $\beta = 0.005$, and (b) $\beta = 0.05$. (c) Is the system stable or unstable in each case? If the system is stable, what is the phase margin?



c. For $\beta = 0.005$,

$$|T(f)| = 1 (0 \text{ dB}) \text{ at } f \approx 2.10 \times 10^4 \text{ Hz}$$

Then

$$\begin{aligned} \phi &= -\tan^{-1}\left(\frac{2.10 \times 10^4}{10^3}\right) - \tan^{-1}\left(\frac{2.10 \times 10^4}{10^4}\right) - \tan^{-1}\left(\frac{2.10 \times 10^4}{10^5}\right) \\ &= -87.27 - 64.54 - 11.86 = -163.7 \end{aligned}$$

System is stable. Phase margin = 16.3°

For $\beta = 0.05$,

$$|T(f)| = 1 (0 \text{ dB}) \text{ at } f \approx 6.44 \times 10^4 \text{ Hz}$$

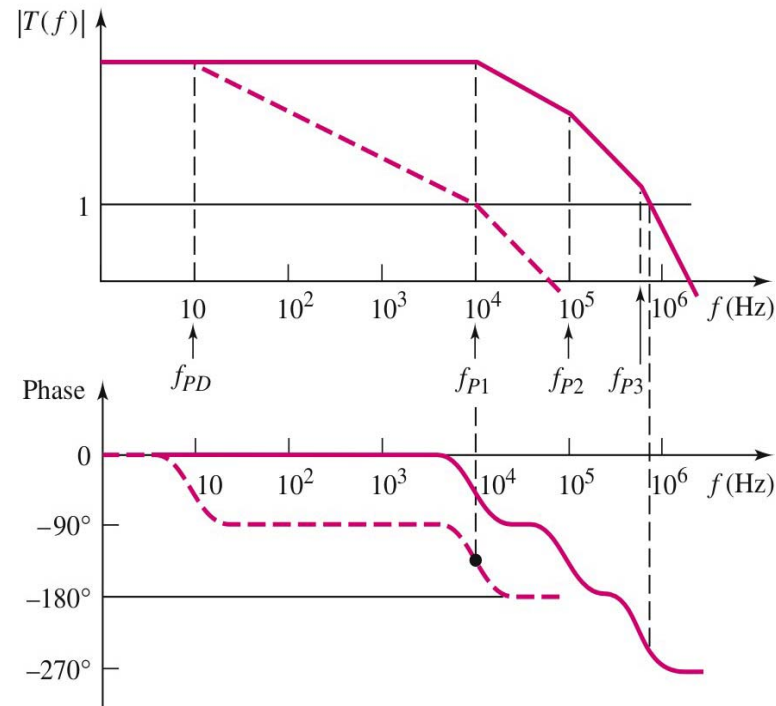
Then

$$\begin{aligned} \phi &= -\tan^{-1}\left(\frac{6.44 \times 10^4}{10^3}\right) - \tan^{-1}\left(\frac{6.44 \times 10^4}{10^4}\right) - \tan^{-1}\left(\frac{6.44 \times 10^4}{10^5}\right) \\ &= -89.11 - 81.17 - 32.78 = -203.1^\circ \Rightarrow \text{System is unstable.} \end{aligned}$$

第十二章 回授與穩定度

12.10 頻率補償

A. 引入新極點



1. 在回路增益中引入一個頻率很低的新極點 f_{PD}
→ 致 $|T(f)| = 1$ 時，使 $|\phi(f)| < 180^\circ$ 。
2. 在引入新極點 f_{PD} 時，假設原始的三個極點不會變動
→ 新的回路增益大小與相位波德圖將如圖中之虛線所示。

第十二章 回授與穩定度

$$A(f) = \frac{A_o}{1 + j \frac{f}{f_{PD}}}$$

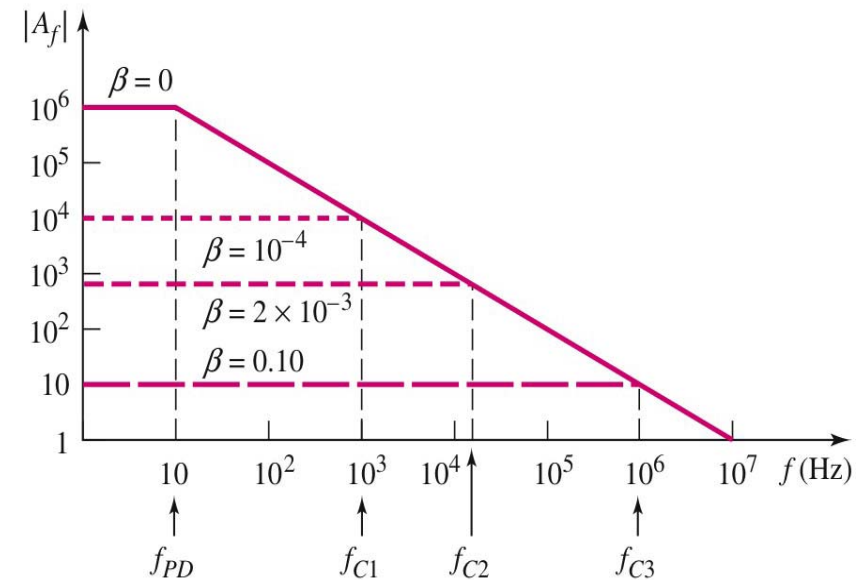
$$A_f(f) = \frac{A(f)}{(1 + \beta A(f))}$$

$$A_f(f) = \frac{A_o}{(1 + \beta A_o)} \times \frac{1}{1 + j \frac{f}{f_{PD}(1 + \beta A_o)}}$$

$$= \frac{A_{fo}}{1 + j \frac{f}{f_{fPD}}}$$

where $A_{fo} = \frac{A_o}{(1 + \beta A_o)}$; $f_{fPD} = f_{PD}(1 + \beta A_o)$

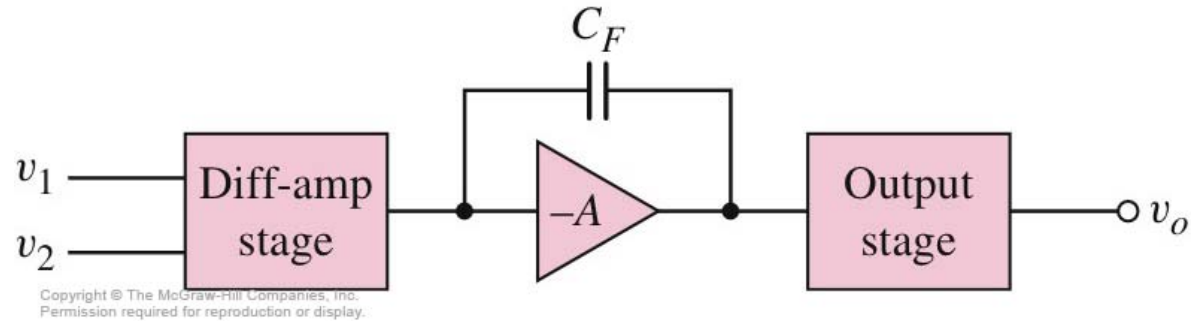
and $A_{fo} \times f_{fPD} = A_o \times f_{PD}$



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第十二章 回授與穩定度

B. 米勒補償技術

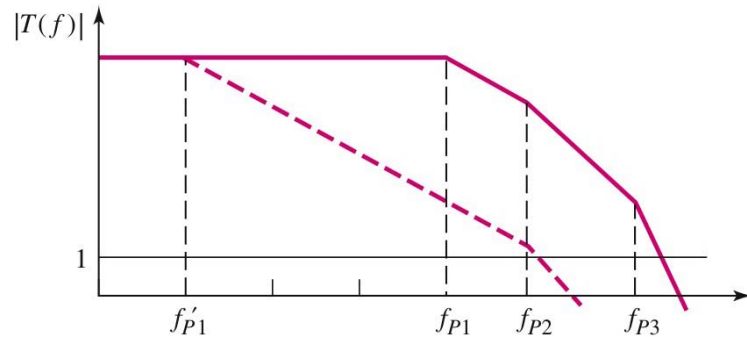


C_F 稱為補償電容

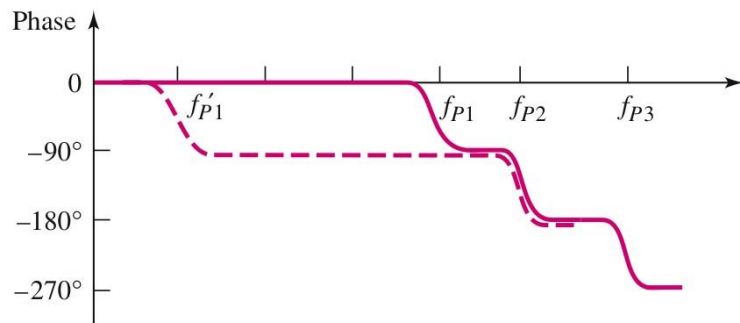
$$C_M = C_F (1 + A)$$

$$f_{P1} = \frac{1}{2\pi R_2 C_M}$$

第十二章 回授與穩定度



1. 米勒補償技術：
移動極點 $f_{P1} \rightarrow f'_{P1}$



2. 在移動極點 f_{P1} 時，
假設其它兩個極點不會變動
→ 使得 $|T(f)|=1$ 之頻率較低，
且 $|\phi| > -180^\circ$ (放大器穩定)。

12.77 A loop gain function is given by

$$T(f) = \frac{500}{\left(1 + j \frac{f}{10^4}\right) \left(1 + j \frac{f}{5 \times 10^4}\right) \left(1 + j \frac{f}{10^5}\right)}$$

- (a) Determine the frequency f_{180} (to a good approximation) at which the phase of $T(f)$ is -180° .
- (b) What is the magnitude of $T(f)$ at the frequency $f = f_{180}$ found in part (a)?
- (c) Insert a dominant pole such that the phase margin is approximately 60° . Assume the original poles are fixed. What is the dominant pole frequency?

$$(a) \quad \phi = -180 = -\tan^{-1}\left(\frac{f_{180}}{10^4}\right) - \tan^{-1}\left(\frac{f_{180}}{5 \times 10^4}\right) - \tan^{-1}\left(\frac{f_{180}}{10^5}\right)$$

$$f_{180} \cong 8.06 \times 10^4 \text{ Hz}$$

$$(b) \quad |T| = \frac{500}{\sqrt{1 + \left(\frac{8.06 \times 10^4}{10^4}\right)^2} \sqrt{1 + \left(\frac{8.06 \times 10^4}{5 \times 10^4}\right)^2} \sqrt{1 + \left(\frac{8.06 \times 10^4}{10^5}\right)^2}}$$

$$= \frac{500}{(8.122)(1.897)(1.284)} = 25.3$$

$$(c) \quad T = \frac{500}{\left(1 + j \frac{f}{f_{PD}}\right) \left(1 + j \frac{f}{10^4}\right) \left(1 + j \frac{f}{5 \times 10^4}\right) \left(1 + j \frac{f}{10^5}\right)}$$

$$\text{Phase Margin} = 60^\circ \Rightarrow \phi = -120^\circ = -\tan^{-1} \frac{f}{f_{PD}} - \tan^{-1} \frac{f}{10^4} - \tan^{-1} \frac{f}{5 \times 10^4} - \tan^{-1} \frac{f}{10^5}$$

$$\text{Assume } \tan^{-1} \frac{f}{f_{PD}} \cong 90^\circ \quad \text{Then } f \cong 4.2 \times 10^3 \text{ Hz}$$

$$|T| = 1 = \frac{500}{\sqrt{1 + \left(\frac{4.2 \times 10^3}{f_{PD}}\right)^2} \sqrt{1 + \left(\frac{4.2 \times 10^3}{10^4}\right)^2} \sqrt{1 + \left(\frac{4.2 \times 10^3}{5 \times 10^4}\right)^2} \sqrt{1 + \left(\frac{4.2 \times 10^3}{10^5}\right)^2}}$$

$$1 = \frac{500}{\sqrt{1 + \left(\frac{4.2 \times 10^3}{f_{PD}}\right)^2} (1.085)(1.004)(1.0)}$$

$$\frac{4.2 \times 10^3}{f_{PD}} \cong \frac{500}{(1.0846)(1.0035)(1.0)}$$

$$f_{PD} = 9.14 \text{ Hz}$$